

# Exercise: Benchmarking Derivative-Free Optimization Algorithms

July 5, 2017

CEA/EDF/Inria summer school "Numerical Analysis"  
Université Pierre-et-Marie-Curie, Paris, France

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CMAP, Ecole Polytechnique



## Requirements:

python 2.6 or 2.7

use Anaconda if not already installed:  
(<https://www.continuum.io/downloads>)

note: python 3.x not yet supported

matplotlib >2.0

in principle via `pip install matplotlib`

otherwise, see <http://matplotlib.org/users/installing.html>

## Objectives of the exercise:

- ① Get acquainted with the COCO platform  
at least with its postprocessing and visualization
- ② Gain insights into data  
of some of the 150+ algorithm data sets of COCO

<https://github.com/numbbo/coco>

numbbo/coco: Numerical ... x +

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code-experiments	A little more verbose error message when suite regression test fails	a month ago
code-postprocessing	Hashes are back on the plots.	a month ago
code-preprocessing	Fixed preprocessing to work correctly with the extended biobjective s...	3 months ago
howtos	Update create-a-suite-howto.md	4 months ago
.clang-format	raising an error in bbob2009_logger.c when best_value is NULL. Plus s...	2 years ago
.hgignore	raising an error in bbob2009_logger.c when best_value is NULL. Plus s...	2 years ago
AUTHORS	small correction in AUTHORS	a year ago
LICENSE	Update LICENSE	11 months ago

<https://github.com/numbbo/coco>

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- .hgignore raising an error in bbob2009\_logger.c when best\_value is NULL. Plus s... 2 years ago
- AUTHORS small correction in AUTHORS a year ago
- LICENSE Update LICENSE 11 months ago

**Step 1: download COCO**

Clone with HTTPS Use Git or checkout with SVN using the web URL.  
<https://github.com/numbbo/coco.git>

Open in Desktop **Download ZIP** 4 months ago

# https://github.com/numbbo/coco

numbbo/coco: Numerical ... x +

GitHub, Inc. (US) https://github.com/numbbo/coco

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2. In a system shell, `cd` into the `coco` or `coco-<version>` folder (framework root), where the file `do.py` can be found. Type, i.e. execute, one of the following commands once

```
python do.py run-c
python do.py run-java
python do.py run-matlab
python do.py run-octave
python do.py run-python
```

depending on which language shall be used to run the experiments. `run-*` will build the respective code and run the example experiment once. The build result and the example experiment code can be found under `code-experiments/build/<language>` (`<language>=matlab` for Octave). `python do.py` lists all available commands.

3. On the computer where experiment data shall be post-processed, run

```
python do.py install-postprocessing
```

to (user-locally) install the post-processing. From here on, `do.py` has done its job and is only needed again for updating the builds to a new release.

4. Copy the folder `code-experiments/build/YOUR-FAVORITE-LANGUAGE` and its content to another location. In Python it is sufficient to copy the file `example_experiment.py`. Run the example experiment (it already is compiled). As the details vary, see the respective read-me's and/or example experiment files:

- C [read me](#) and [example experiment](#)
- Java [read me](#) and [example experiment](#)

**Step 2:  
installation of post-processing**

http://coco.gforge.inria.fr/doku.php?id=algorithms

## Step 3: downloading data

[[algorithms]]

COMPARING CONTINUOUS OPTIMISERS: COCO

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The following table lists all algorithms related to the BBOB workshops and special sessions in the years 2009 till 2015 together with links to their data. In order to sort the table according to some columns, please click on the corresponding table header. If available, the source codes of the algorithms can be downloaded by clicking on the link with the corresponding algorithm name in the second column.

No	Algorithm	Year	Author(s)	Data Noiseless (Raw)	Data Noisy (Raw)	related PDFs and Remarks
1	ALPS	2009	Hornby	noiselessData	noisyData	PDF
2	AMALGAM	2009	Bosman et al.	noiselessData	noisyData	PDFnoiseless  PDFnoisy
3	BAYEDA	2009	Gallagher	noiselessData	noisyData	PDFnoiseless  PDFnoisy
4	BFGS	2009	Ros	noiselessData	noisyData	PDFnoiseless  PDFnoisy
5	BIPOP-CMA-ES	2009	Hansen	noiselessData	noisyData	PDFnoiseless  PDFnoisy
6	Cauchy-EDA	2009	Pošik	noiselessData	n/a	PDF
7	CMA-ESPLUSSEL	2009	Auger and Hansen	noiselessData	noisyData	PDFnoiseless  PDFnoisy
8	DASA	2009	Korošec and Šilc	noiselessData	noisyData	PDFnoiseless  PDFnoisy
9	DE-PSO	2009	García-Nieto et al.	noiselessData	noisyData	PDFnoiseless  PDFnoisy
10	DIRECT	2009	Pošik	noiselessData	n/a	PDF algorithm is deterministic and thus, only run on each instance once
11	EDA-PSO	2009	El-Abd Kamel and	noiselessData	noisyData	PDF

for the moment:  
IPOP-CMA-ES  
(algorithm 56)

Search

### Navigation

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- new code homepage
- download new code directly
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- BBOB 2015 @ GECCO
- Algorithms

- Schedule
- Downloads
- BBOB 2012
  - Algorithms
  - Results
  - Downloads
- BBOB 2010

https://github.com/numbbo/coco

coco/README.md at devel... x

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Another entry point for your own experiments can be the `code-experiments/examples` folder.

- Now you can run your favorite algorithm on the `bbob` suite (for single-objective algorithms) or on the `bbob-biobj` and `bbob-biobj-ext` suites (for multi-objective algorithms). Output is automatically generated in the specified data `result_folder`. By now, more suites might be available, see below.
- Postprocess the data from the results folder by typing

```
python -m cocopp [-o OUTPUT_FOLDERNAME] YOURDATAFOLDER [MORE_DATAFOLDERS]
```

Any subfolder in the folder arguments will be searched for logged data. That is, experiments from different batches can be in different folders collected under a single "root" `YOURDATAFOLDER` folder. We can also compare more than one algorithm by

**postprocess**

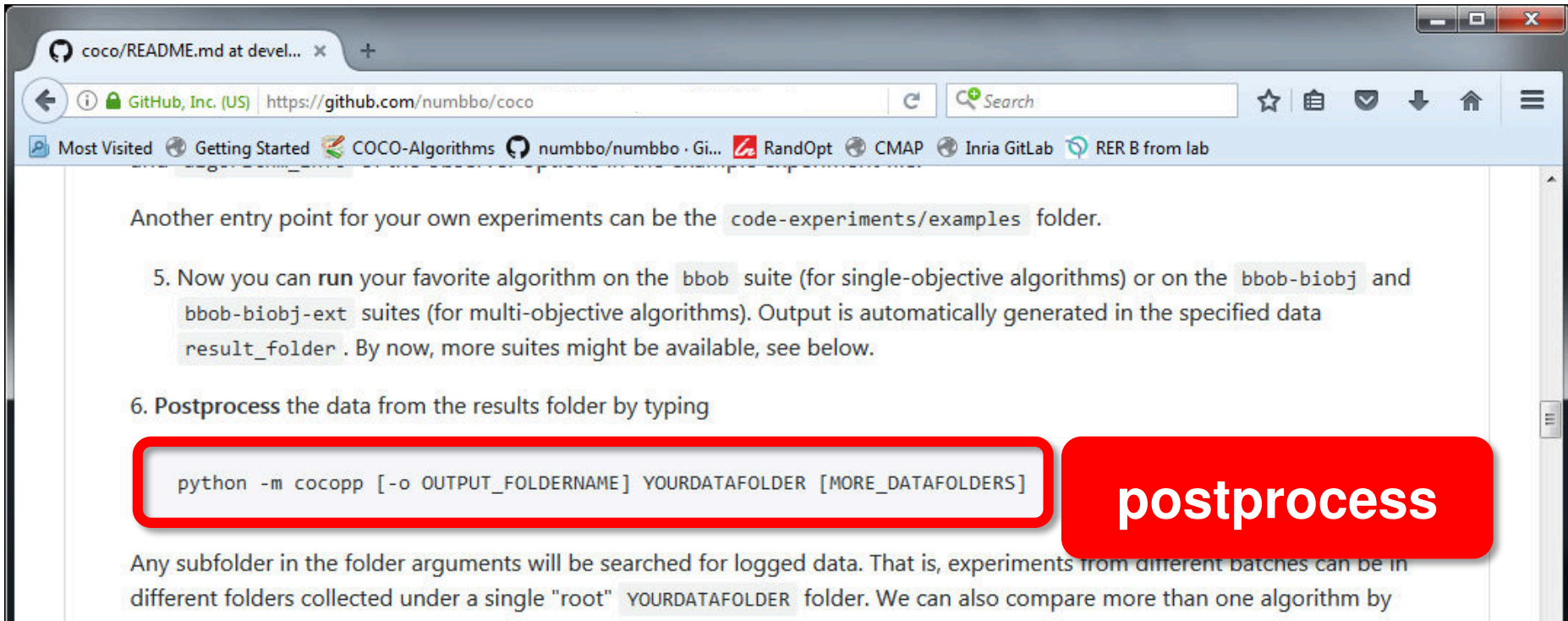
```
python -m cocopp IPOP-CMA-ES_ros_noiseless.tar.gz
```

A summary pdf can be produced via LaTeX. The corresponding templates can be found in the `code-postprocessing/latex-templates` folder. Basic html output is also available in the result folder of the postprocessing (file `templateBBOBarticle.html`).

- Once your algorithm runs well, increase the budget in your experiment script, if necessary implement randomized independent restarts, and follow the above steps successively until you are happy.
- The experiments can be parallelized with any re-distribution of single problem instances to batches (see `example_experiment.py` for an example). Each batch must write in a different target folder (this should happen



<https://github.com/numbbo/coco>



Another entry point for your own experiments can be the `code-experiments/examples` folder.

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```
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**postprocess**

```
python -m cocopp IPOP-CMA-ES_ros_noiseless.tar.gz
```

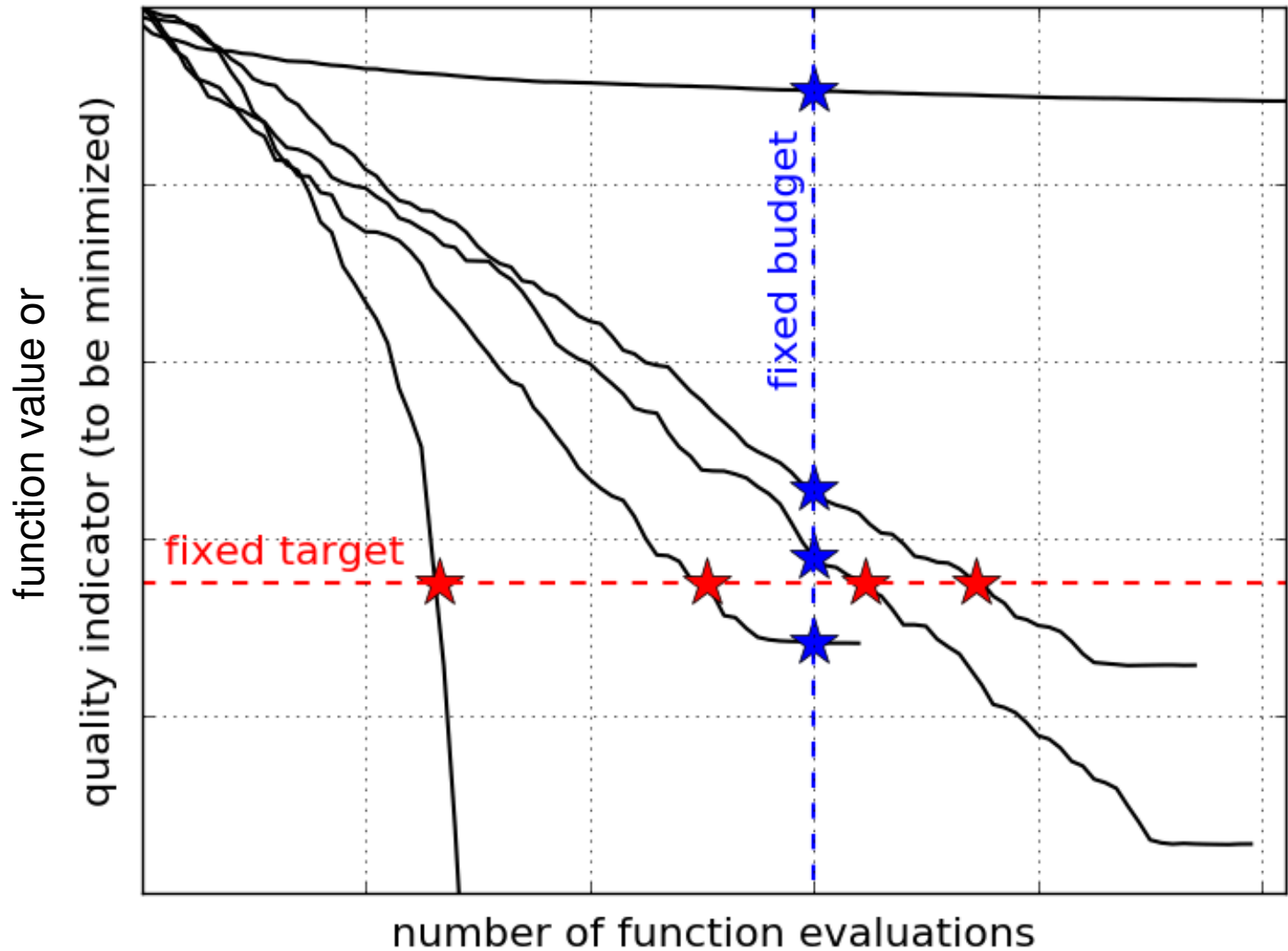
**Alternative within (I)python:**

```
> import cocopp
```

```
> cocopp.main("IPOP-CMA-ES_ros_noiseless.tar.gz")
```

**Reminder:**  
**Measuring Performance Empirically**

convergence graphs is all we have to start with...

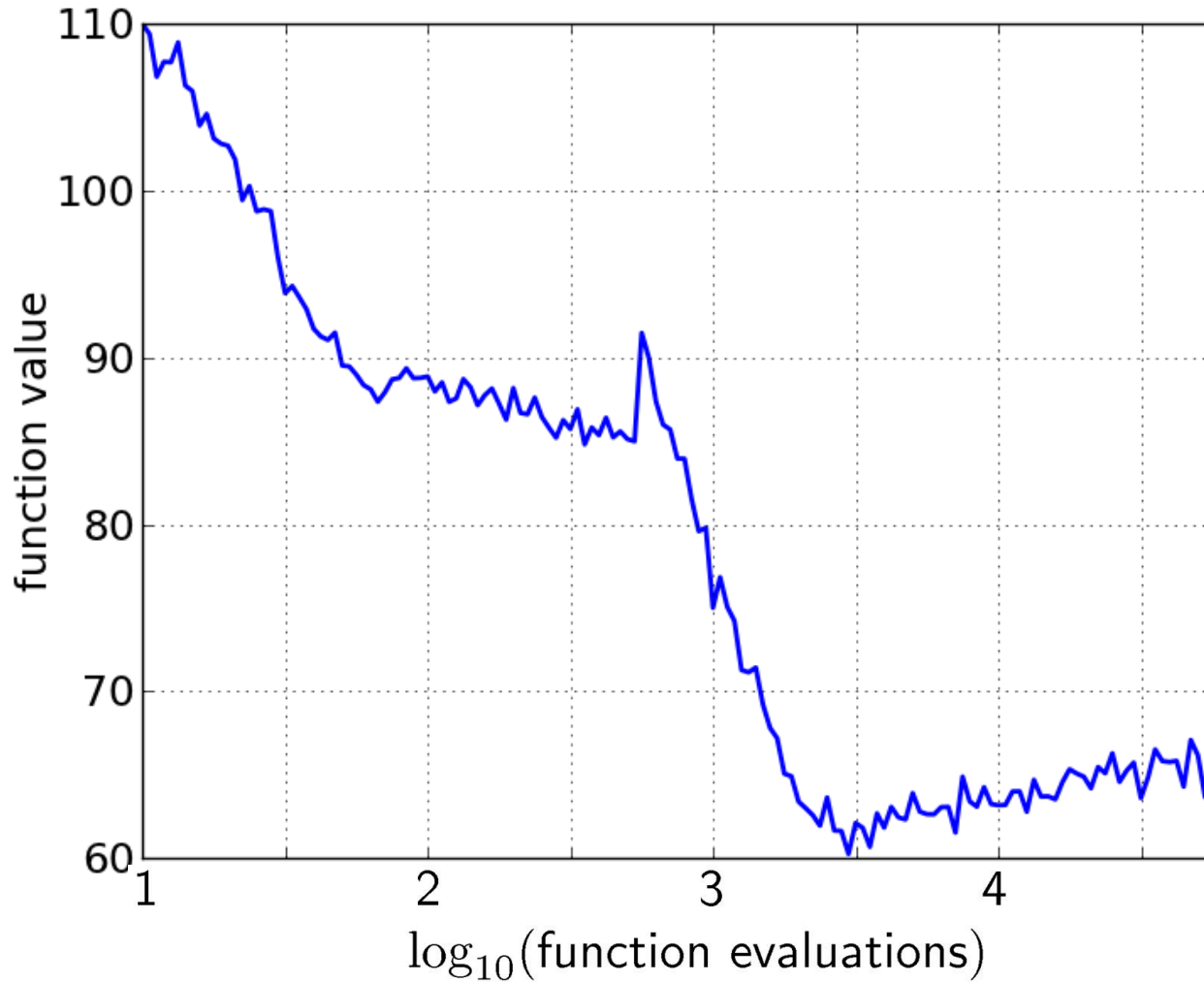


**ECDF:**

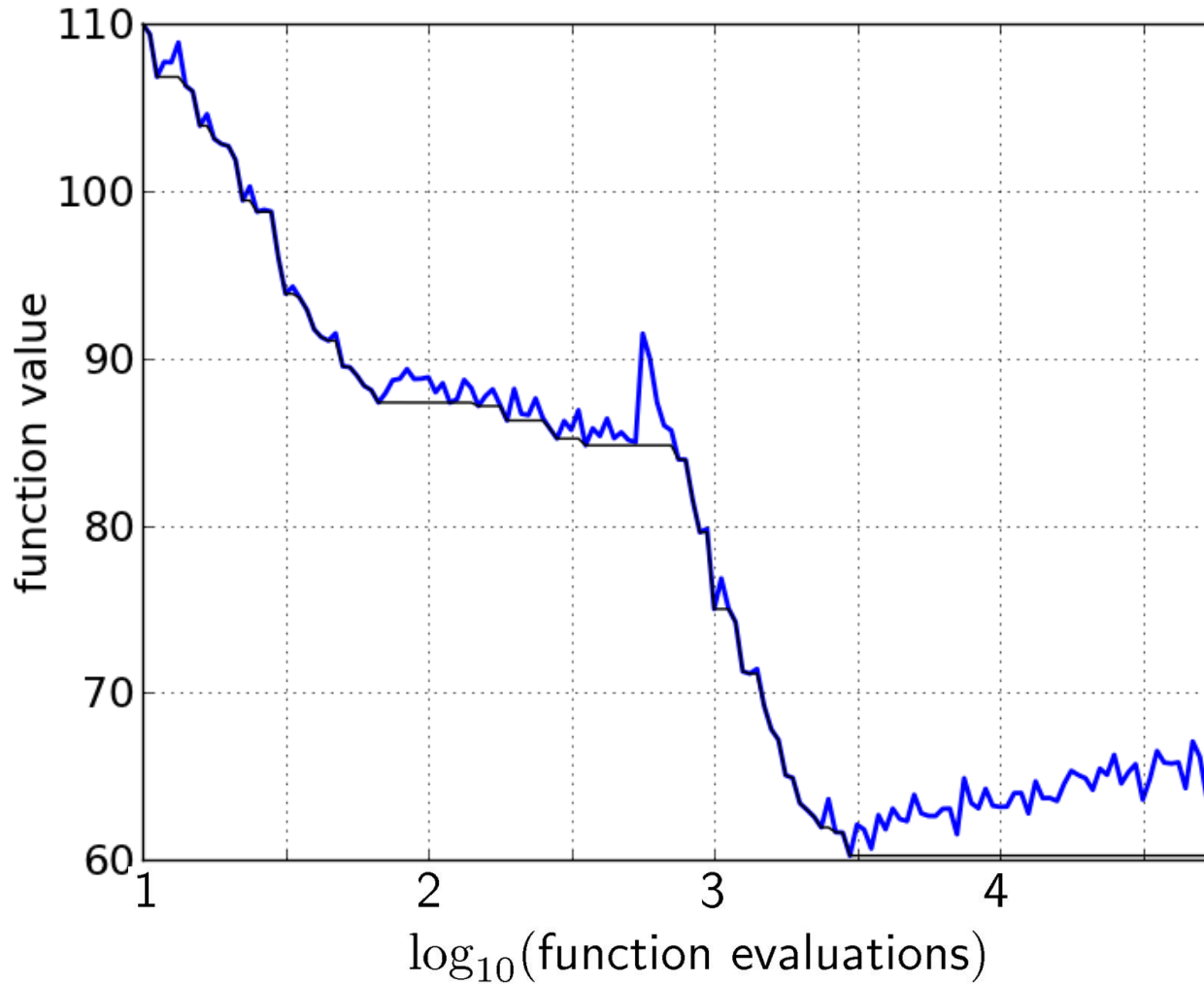
Empirical Cumulative Distribution Function of the  
Runtime

[aka data profile]

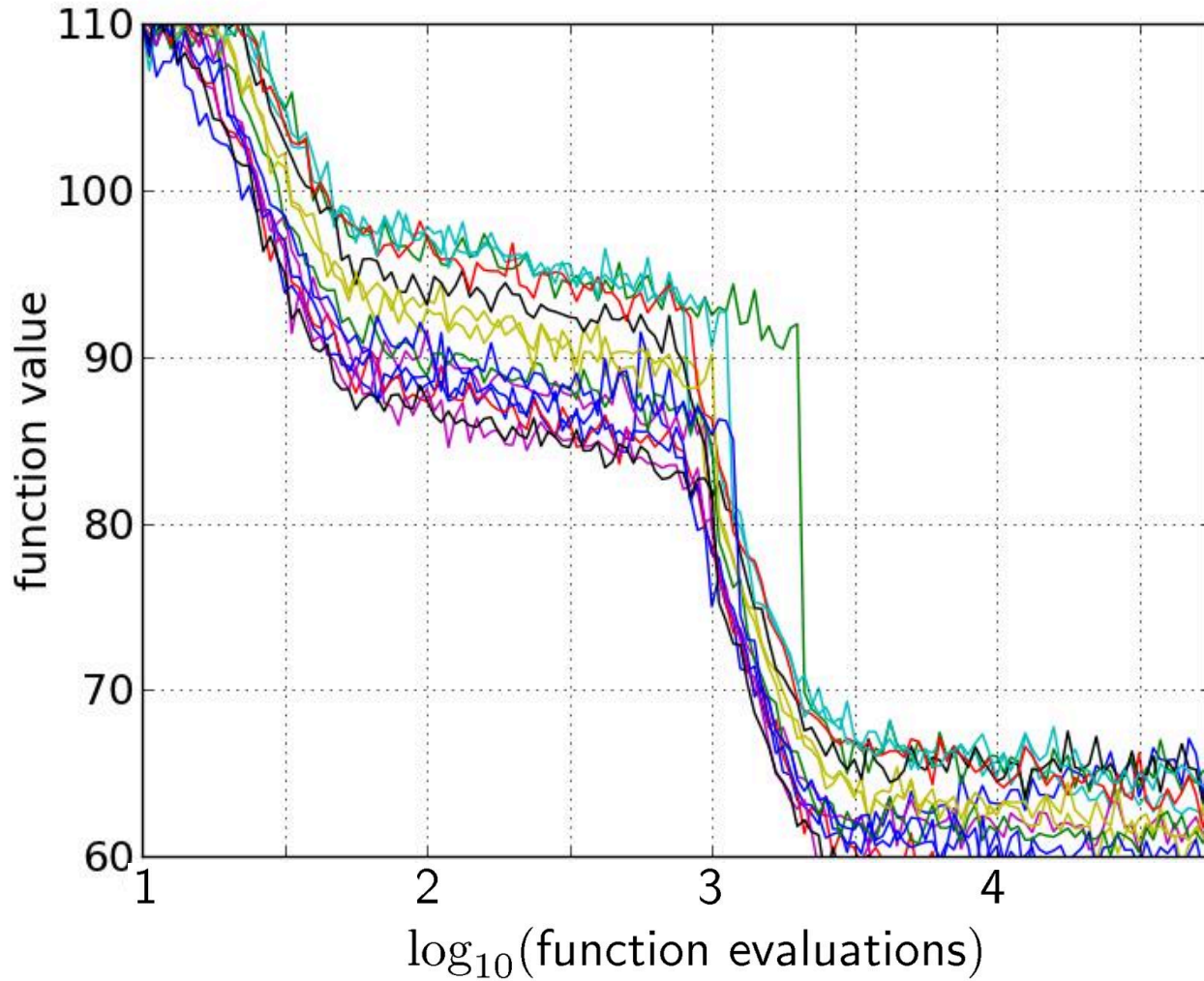
# A Convergence Graph



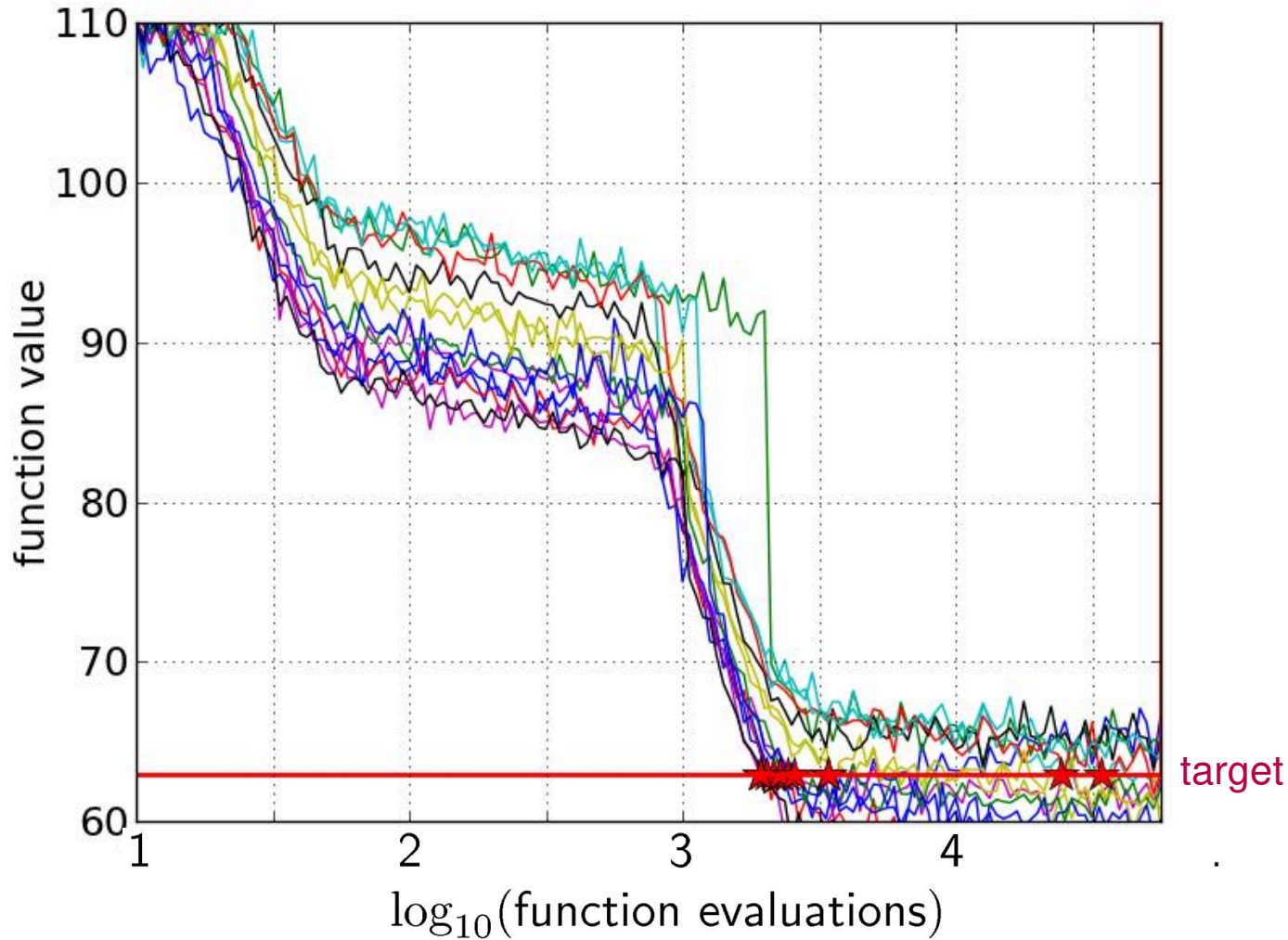
# First Hitting Time is Monotonous



# 15 Runs

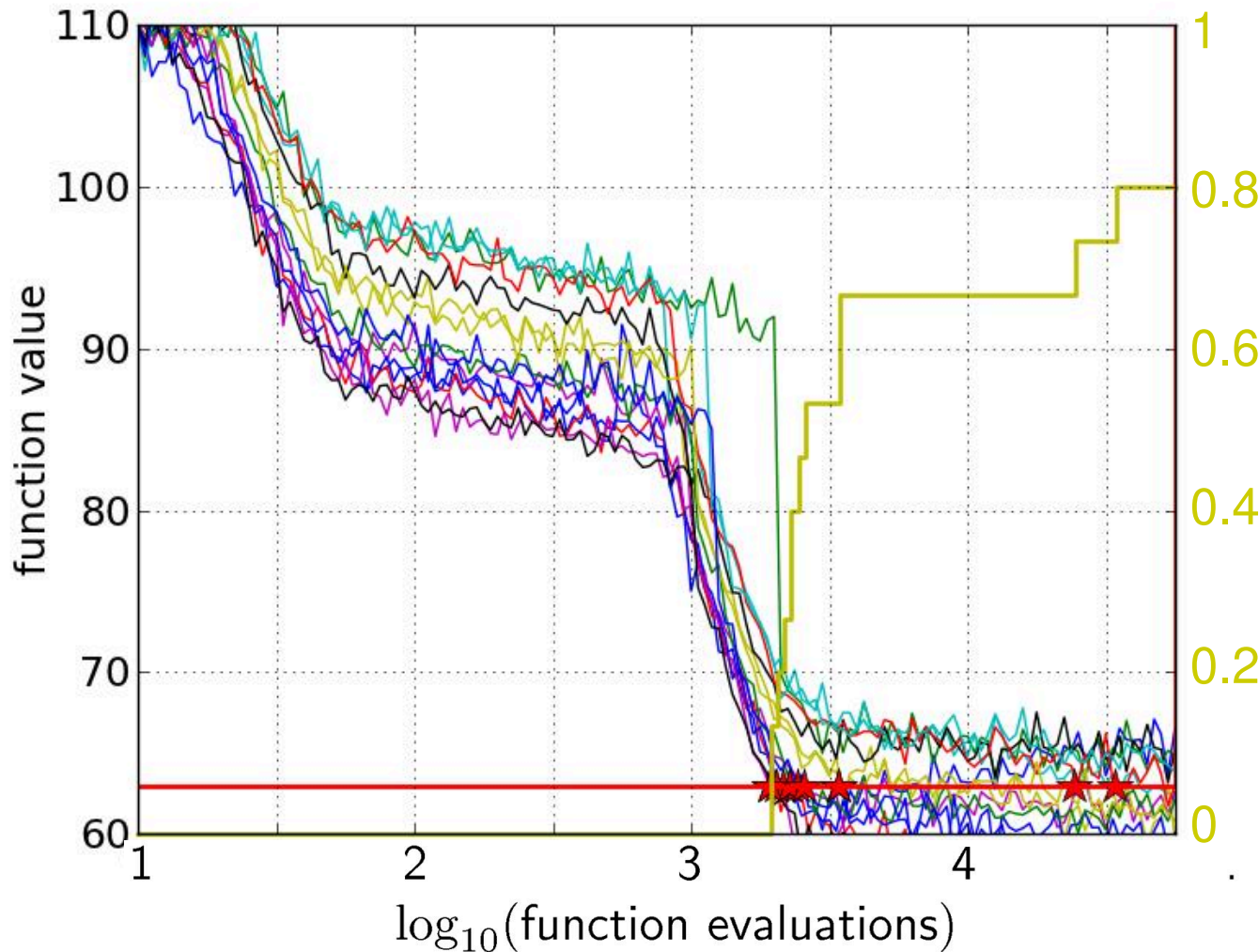


# 15 Runs $\leq$ 15 Runtime Data Points



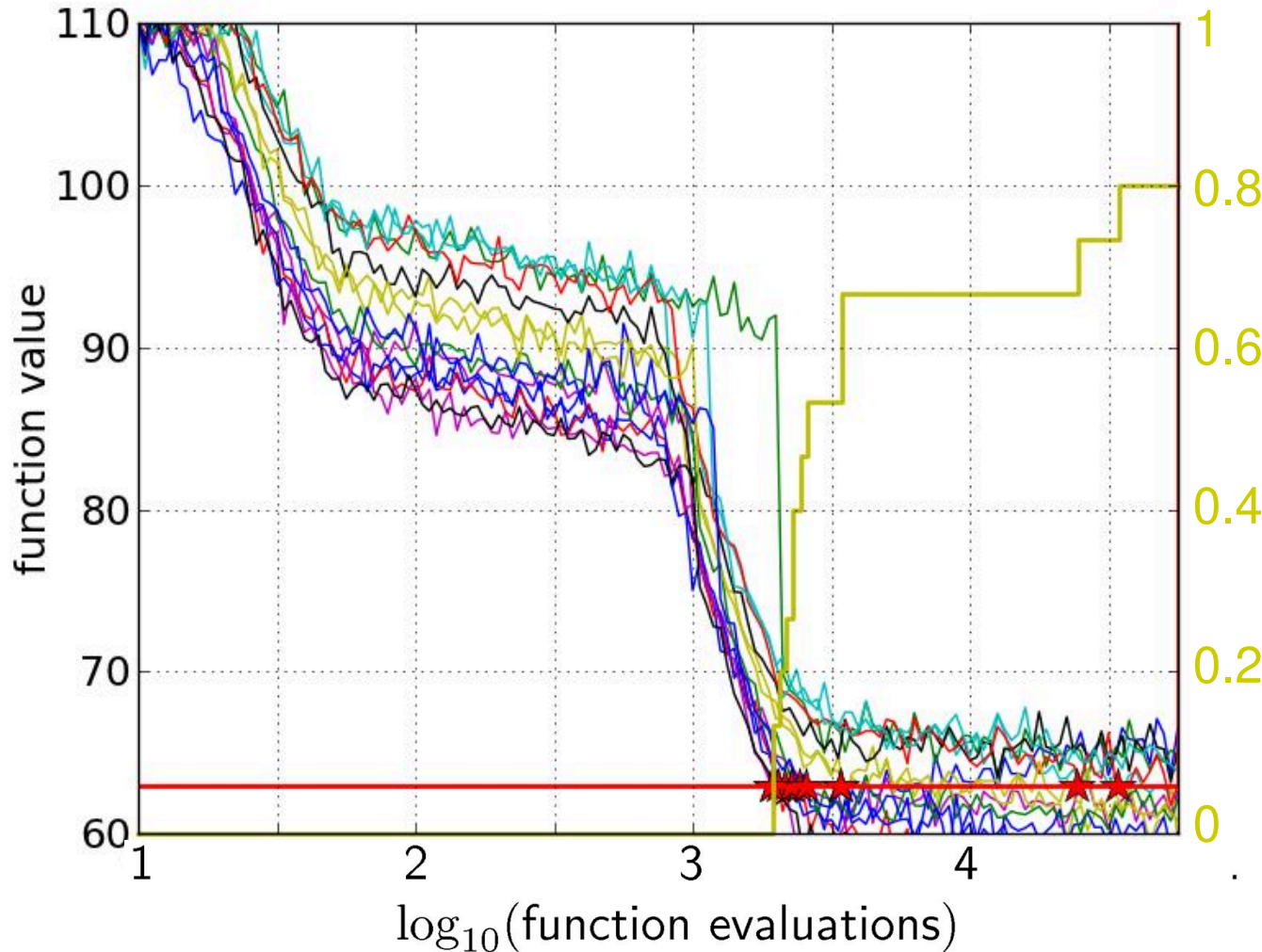


# Empirical Cumulative Distribution



- 1 the **ECDF** of run lengths to reach the target
  - has for each data point a **vertical step of constant size**
  - displays for each x-value (budget) the count of observations to the left (first hitting times)

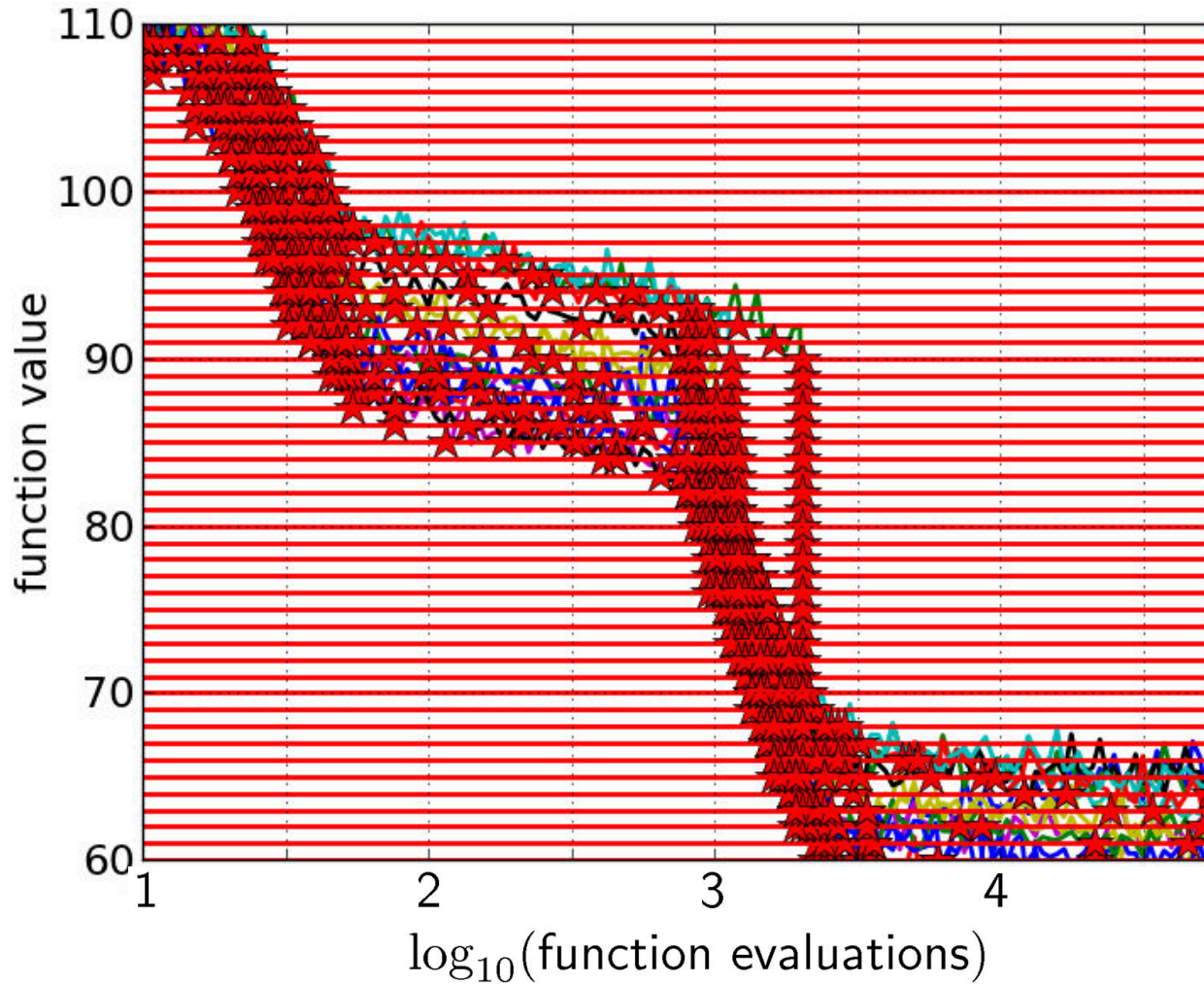
# Empirical Cumulative Distribution



- the higher the better (= more targets solved)

- the more to the left the better (= targets solved quicker)

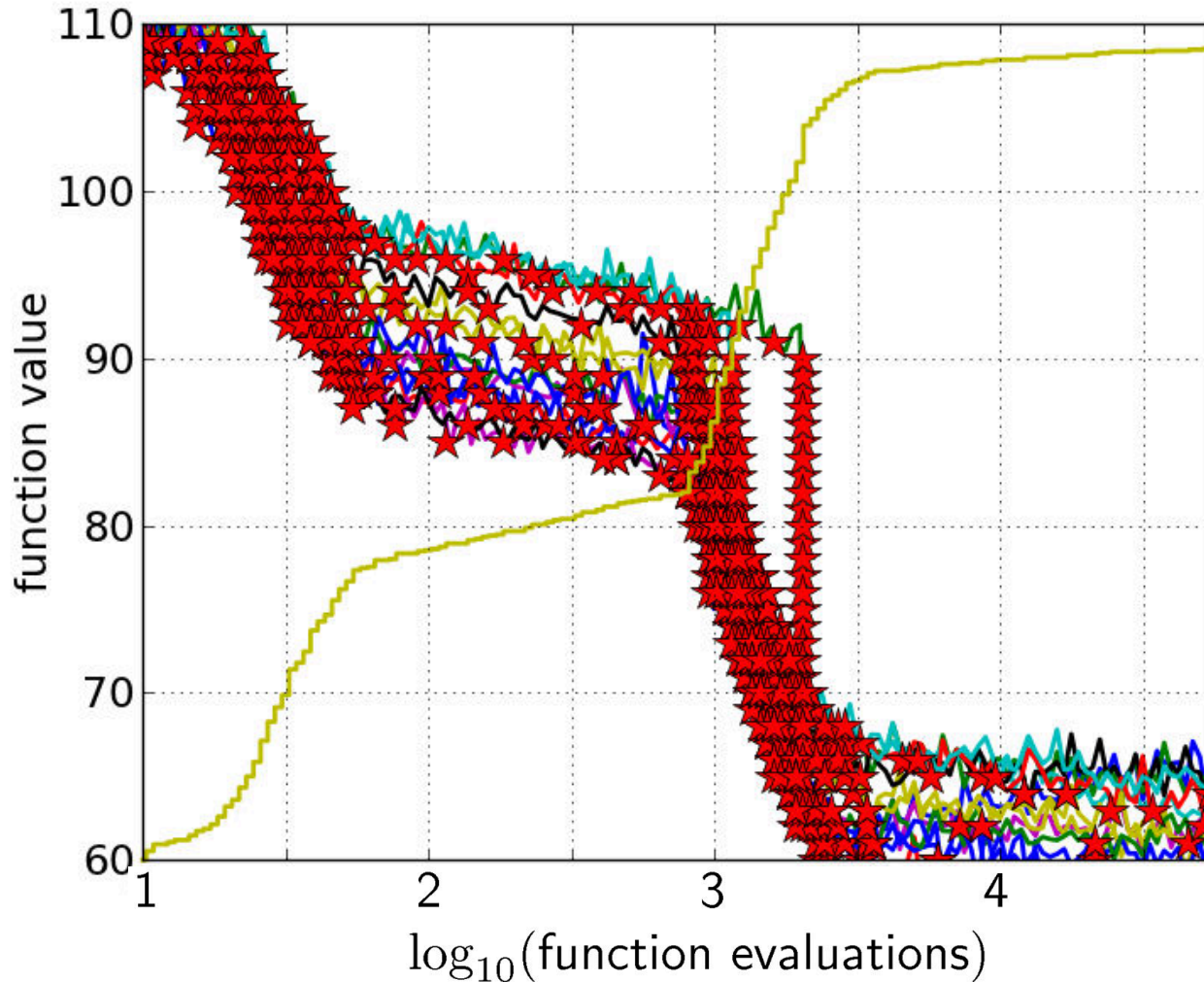
# Aggregation



15 runs

50 targets

# Aggregation

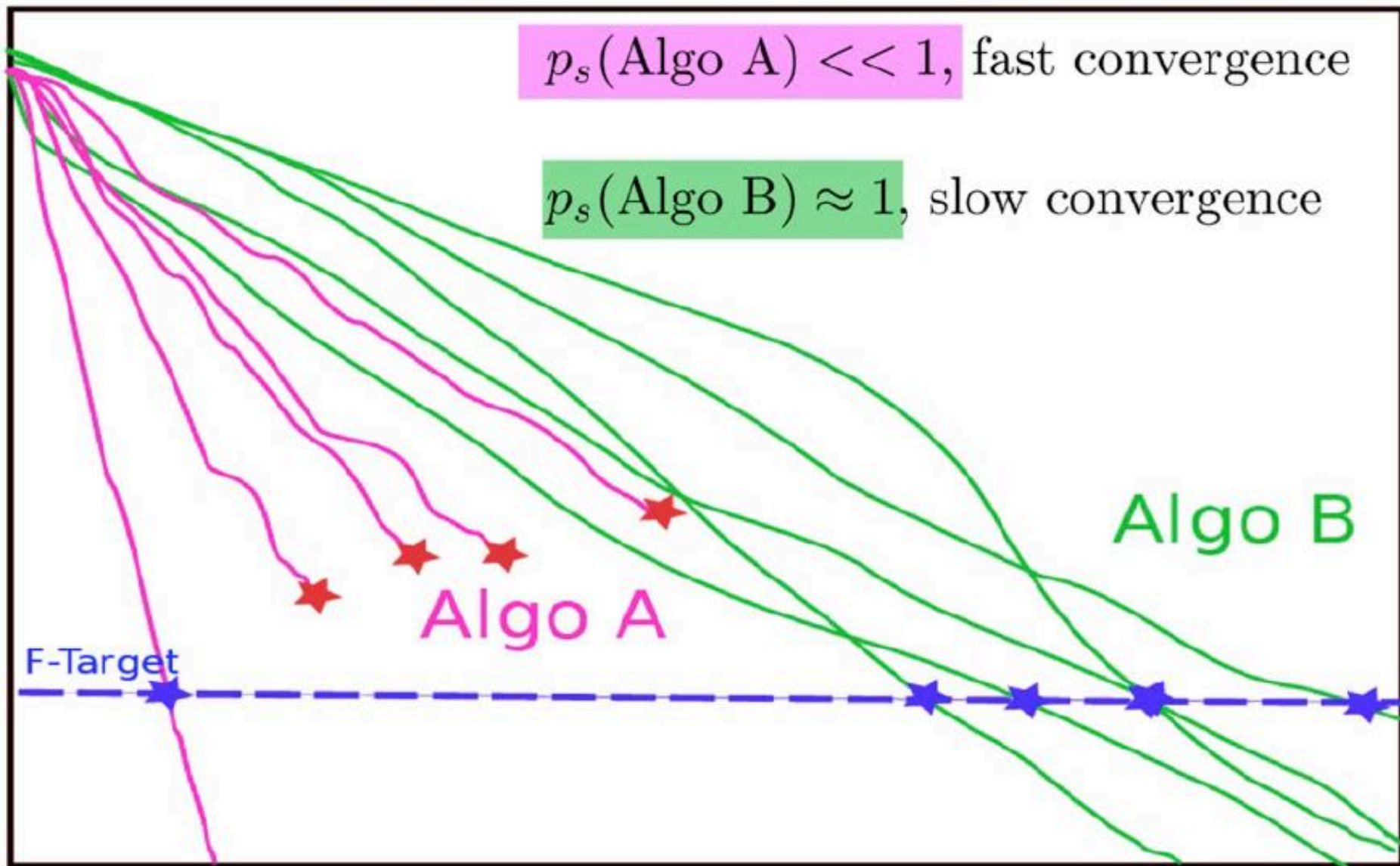


15 runs

50 targets

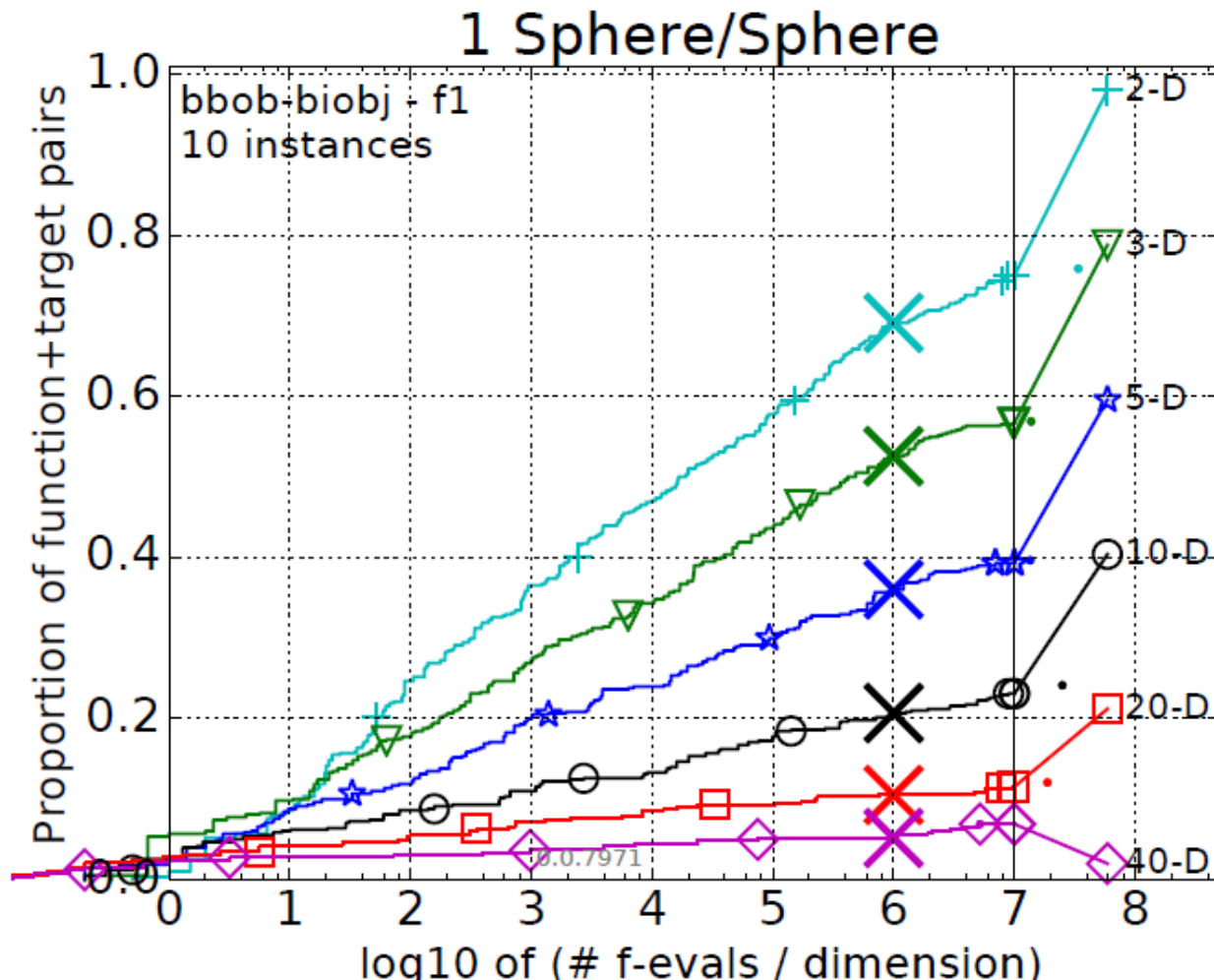
ECDF with 750  
steps

# Fixed-target: Simulated Restarts



# ECDFs with Simulated Restarts

What we typically plot are ECDFs of the simulated restarted algorithms:



# Exercise

## Objective:

investigate the performance of algorithms, available at

<http://coco.gforge.inria.fr/doku.php?id=algorithms>

- 56 IPOP-CMA-ES: CMA-ES with restarts and increasing popsize
- 5 BIPOP-CMA-ES: two different popsize regimes
- 22 Nelder-Mead simplex (use better "NelderDoerr" version here)
- 4 BFGS: quasi-Newton
- 14 Genetic Algorithm: discretization of cont. variables ("GA")
- 25 ONEFIFTH: (1+1)-ES with 1/5 rule

postprocess (now) and investigate the data (after a few more slides)















tip: use `--omit-single` option to save time











# **The single-objective BBOB functions**



# The bbob Testbed

- 24 functions in 5 groups:

1 Separable Functions	
f1	 Sphere Function
f2	 Ellipsoidal Function
f3	 Rastrigin Function
f4	 Büche-Rastrigin Function
f5	 Linear Slope
2 Functions with low or moderate conditioning	
f6	 Attractive Sector Function
f7	 Step Ellipsoidal Function
f8	 Rosenbrock Function, original
f9	 Rosenbrock Function, rotated
3 Functions with high conditioning and unimodal	
f10	 Ellipsoidal Function
f11	 Discus Function
f12	 Bent Cigar Function
f13	 Sharp Ridge Function
f14	 Different Powers Function

4 Multi-modal functions with adequate global structure	
f15	 Rastrigin Function
f16	 Weierstrass Function
f17	 Schaffers F7 Function
f18	 Schaffers F7 Functions, moderately ill-conditioned
f19	 Composite Griewank-Rosenbrock Function F8F2
5 Multi-modal functions with weak global structure	
f20	 Schwefel Function
f21	 Gallagher's Gaussian 101-me Peaks Function
f22	 Gallagher's Gaussian 21-hi Peaks Function
f23	 Katsuura Function
f24	 Lunacek bi-Rastrigin Function

- 6 dimensions: 2, 3, 5, 10, 20, (40 optional)

# Notion of Instances

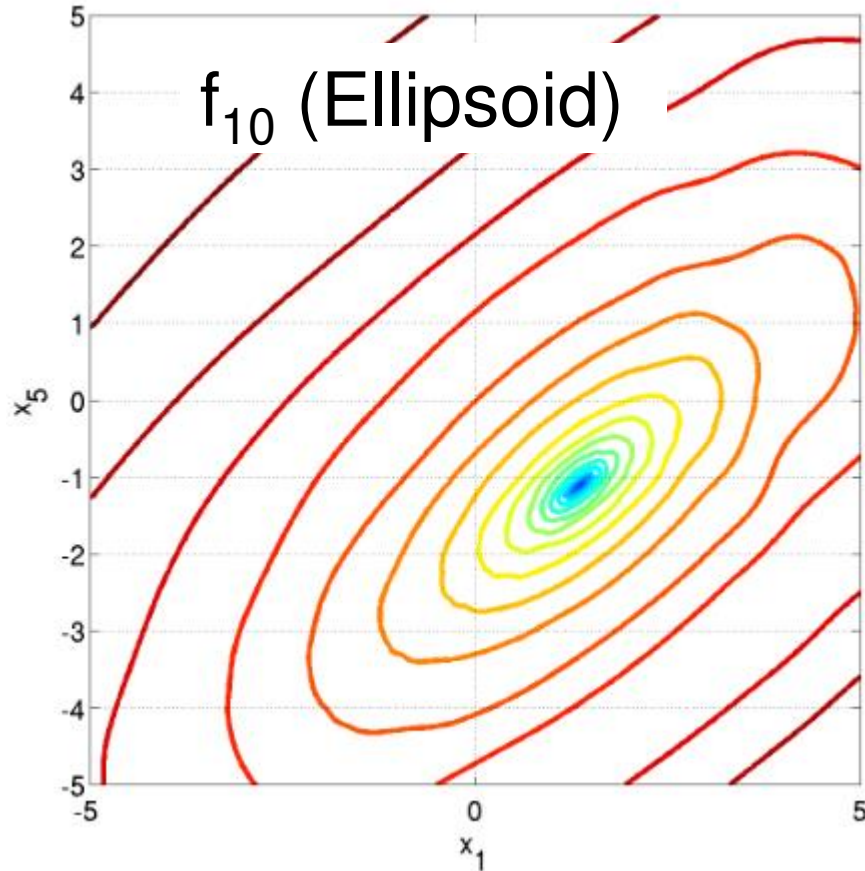
- All COCO problems come in form of instances
  - e.g. as translated/rotated versions of the same function
- Prescribed instances typically change from year to year
  - avoid overfitting
  - 5 instances are always kept the same

Plus:

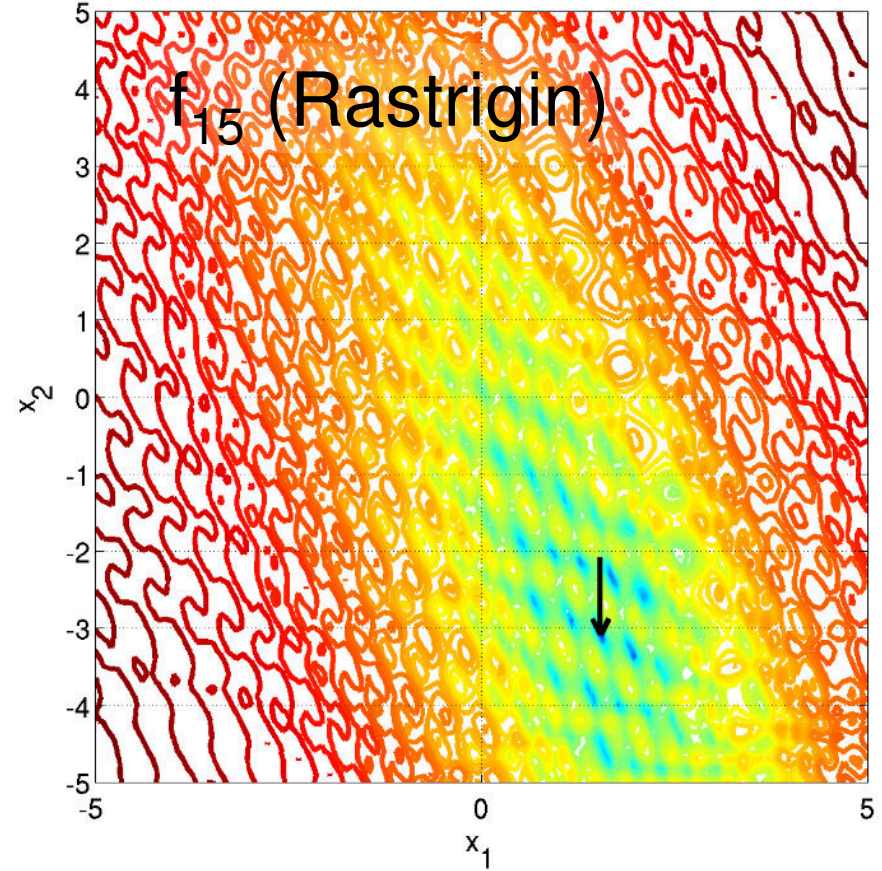
- the bbob functions are locally perturbed by non-linear transformations

# Notion of Instances

All COCO problems come in form of instances



linear transformations



# The single-objective **noisy** BBOB functions

# bbob-noisy Testbed

- 30 functions with various kinds of noise types and strengths
  - 3 noise types: Gaussian, uniform, and seldom Cauchy
  - Functions with moderate noise
  - Functions with severe noise
  - Highly multi-modal functions with severe noise
  - **bbob** functions included: Sphere, Rosenbrock, Step ellipsoid, Ellipsoid, Different Powers, Schaffers' F7, Composite Griewank-Rosenbrock
- 6 dimensions: 2, 3, 5, 10, 20, (40 optional)

**COCO extended to  
multiobjective optimization**

# bbob-biobj Testbed

- **55 functions** by combining 2 bbob functions

1 Separable Functions	
f1	<input type="checkbox"/> Sphere Function ✓
f2	<input type="checkbox"/> Ellipsoidal Function ✓
f3	<input type="checkbox"/> Rastrigin Function
f4	<input type="checkbox"/> Büche-Rastrigin Function
f5	<input type="checkbox"/> Linear Slope
2 Functions with low or moderate conditioning	
f6	<input type="checkbox"/> Attractive Sector Function ✓
f7	<input type="checkbox"/> Step Ellipsoidal Function
f8	<input type="checkbox"/> Rosenbrock Function, original ✓
f9	<input type="checkbox"/> Rosenbrock Function, rotated
3 Functions with high conditioning and unimodal	
f10	<input type="checkbox"/> Ellipsoidal Function
f11	<input type="checkbox"/> Discus Function
f12	<input type="checkbox"/> Bent Cigar Function
f13	<input type="checkbox"/> Sharp Ridge Function ✓
f14	<input type="checkbox"/> Different Powers Function ✓

4 Multi-modal functions with adequate global structure	
f15	<input type="checkbox"/> Rastrigin Function ✓
f16	<input type="checkbox"/> Weierstrass Function
f17	<input type="checkbox"/> Schaffers F7 Function ✓
f18	<input type="checkbox"/> Schaffers F7 Functions, moderately ill-conditioned
f19	<input type="checkbox"/> Composite Griewank-Rosenbrock Function F8F2
5 Multi-modal functions with weak global structure	
f20	<input type="checkbox"/> Schwefel Function ✓
f21	<input type="checkbox"/> Gallagher's Gaussian 101-me Peaks Function ✓
f22	<input type="checkbox"/> Gallagher's Gaussian 21-hi Peaks Function
f23	<input type="checkbox"/> Katsuura Function
f24	<input type="checkbox"/> Lunacek bi-Rastrigin Function

# bbob-biobj Testbed

- 55 functions by combining 2 bbob functions

1 Separable Functions		4 Multi-modal functions with adequate global structure									
f1	<input checked="" type="checkbox"/> Sphere Function ✓	f15	<input checked="" type="checkbox"/> Rastrigin Function ✓								
f2	<input checked="" type="checkbox"/> Ellipsoidal Function ✓	f16	<input type="checkbox"/> Weierstrass Function								
f3	<input type="checkbox"/> Rastrigin Function	f17	<input checked="" type="checkbox"/> Schaffers F7 Function ✓								
f4	<input type="checkbox"/> Büche-Rastrigin Function										
f5	<input type="checkbox"/> Linear Slope										
2 Functions with low or moderate conditioning											
f6	<input checked="" type="checkbox"/> Attractive Sector Function ✓	$f_1$	$f_2$	$f_6$	$f_8$	$f_{13}$	$f_{14}$	$f_{15}$	$f_{17}$	$f_{20}$	$f_{21}$
f7	<input type="checkbox"/> Step Ellipsoidal Function	$f_1$	<a href="#">f1</a>	<a href="#">f2</a>	<a href="#">f3</a>	<a href="#">f4</a>	<a href="#">f5</a>	<a href="#">f6</a>	<a href="#">f7</a>	<a href="#">f8</a>	<a href="#">f9</a>
f8	<input checked="" type="checkbox"/> Rosenbrock Function, original ✓	$f_2$		<a href="#">f11</a>	<a href="#">f12</a>	<a href="#">f13</a>	<a href="#">f14</a>	<a href="#">f15</a>	<a href="#">f16</a>	<a href="#">f17</a>	<a href="#">f18</a>
f9	<input type="checkbox"/> Rosenbrock Function, rotated	$f_6$			<a href="#">f20</a>	<a href="#">f21</a>	<a href="#">f22</a>	<a href="#">f23</a>	<a href="#">f24</a>	<a href="#">f25</a>	<a href="#">f26</a>
3 Functions with high conditioning and unimodal		$f_8$				<a href="#">f28</a>	<a href="#">f29</a>	<a href="#">f30</a>	<a href="#">f31</a>	<a href="#">f32</a>	<a href="#">f33</a>
f10	<input type="checkbox"/> Ellipsoidal Function	$f_{13}$					<a href="#">f35</a>	<a href="#">f36</a>	<a href="#">f37</a>	<a href="#">f38</a>	<a href="#">f39</a>
f11	<input type="checkbox"/> Discus Function	$f_{14}$						<a href="#">f41</a>	<a href="#">f42</a>	<a href="#">f43</a>	<a href="#">f44</a>
f12	<input type="checkbox"/> Bent Cigar Function	$f_{15}$							<a href="#">f46</a>	<a href="#">f47</a>	<a href="#">f48</a>
f13	<input checked="" type="checkbox"/> Sharp Ridge Function ✓	$f_{17}$								<a href="#">f50</a>	<a href="#">f51</a>
f14	<input checked="" type="checkbox"/> Different Powers Function ✓	$f_{20}$									<a href="#">f53</a>
		$f_{21}$									<a href="#">f54</a>
											<a href="#">f55</a>



# bbob-biobj Testbed

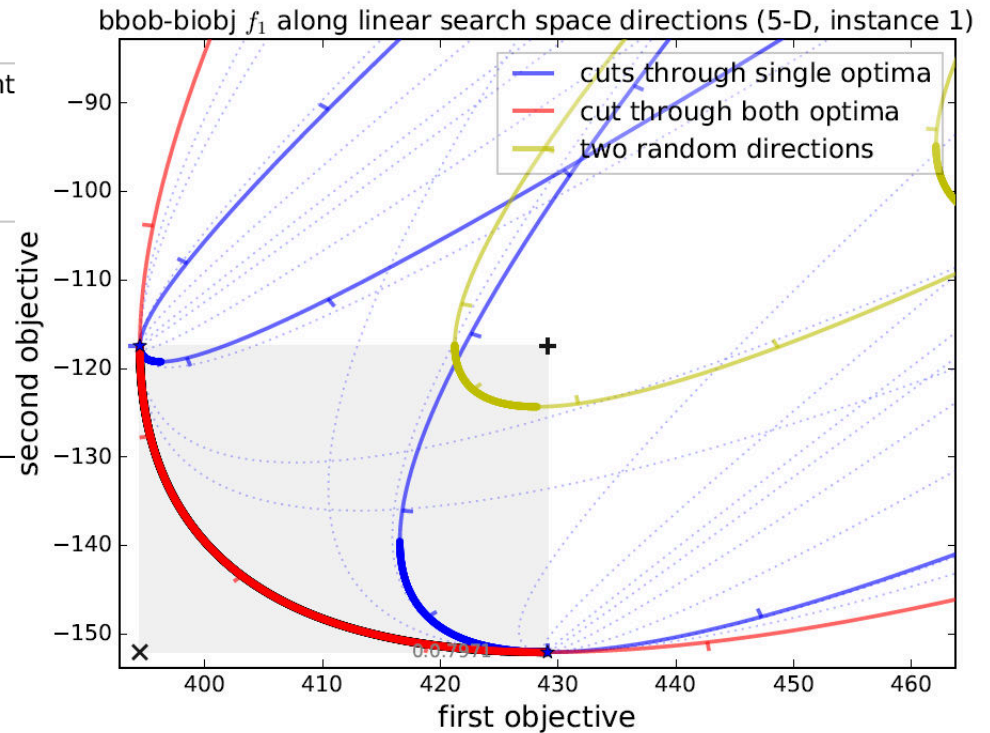
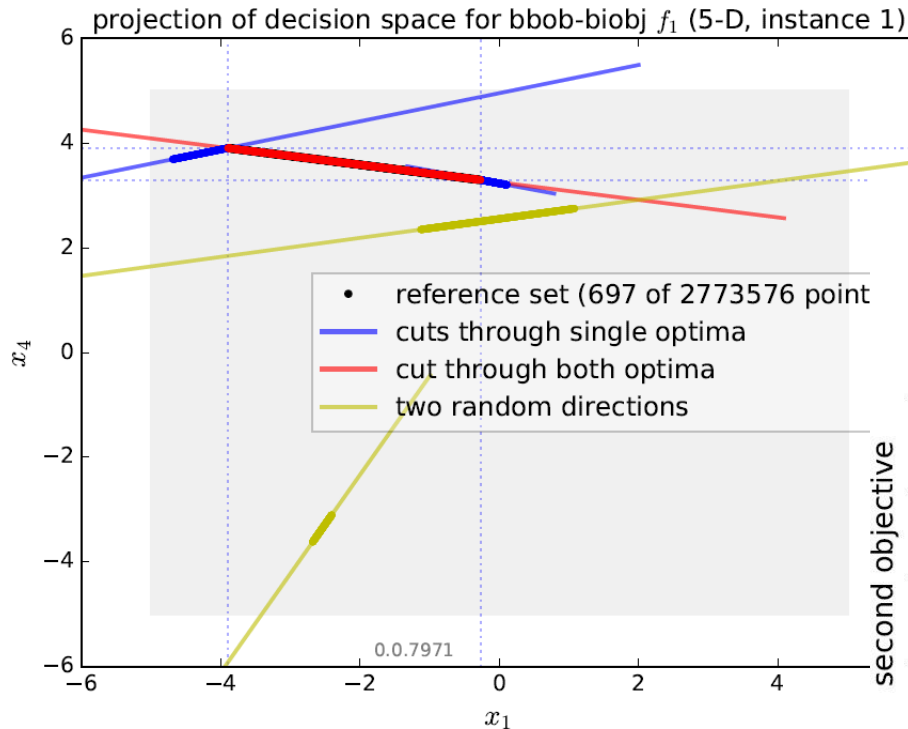
- **55 functions** by combining 2 bbob functions
- **15 function groups** with 3-4 functions each
  - separable – separable, separable – moderate, separable – ill-conditioned, ...
- **6 dimensions**: 2, 3, 5, 10, 20, (40 optional)
- instances derived from bbob instances:
  - more or less  $2i+1$  for 1st objective and  $2i+2$  for 2nd objective
  - exceptions: instances 1 and 2 and when optima are too close
- **no normalization** (algo has to cope with different orders of magnitude)
- for performance assessment: **ideal/nadir points known**

# bbob-biobj Testbed (cont'd)

- Pareto set and Pareto front **unknown**
  - but we have a good idea of where they are by running quite some algorithms and keeping track of all non-dominated points found so far
- Various types of shapes

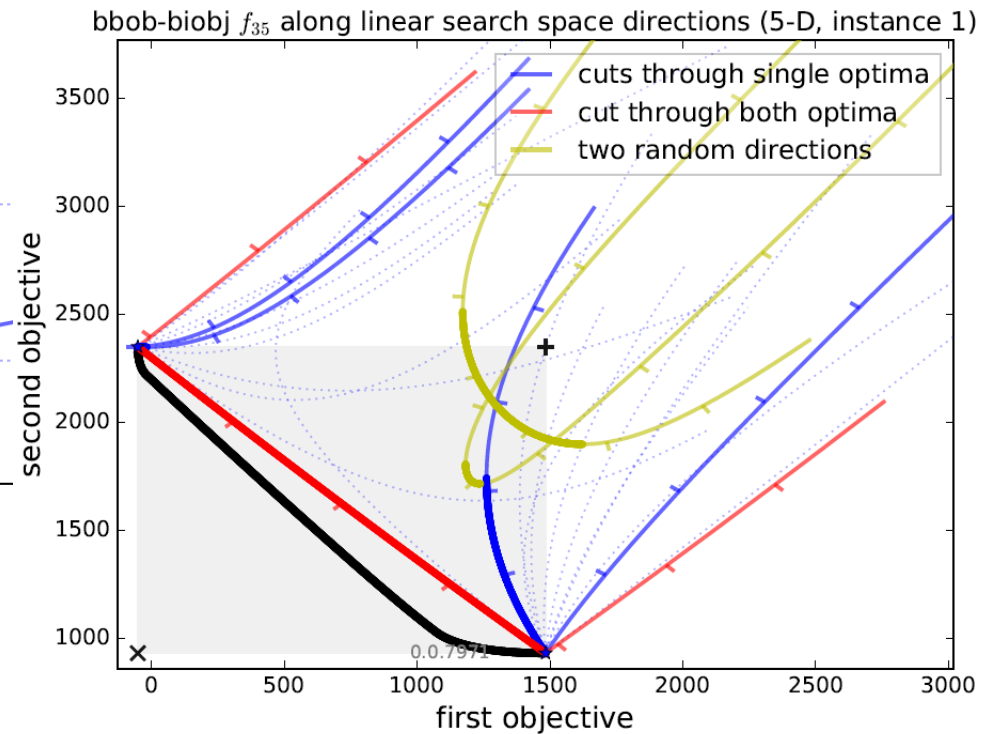
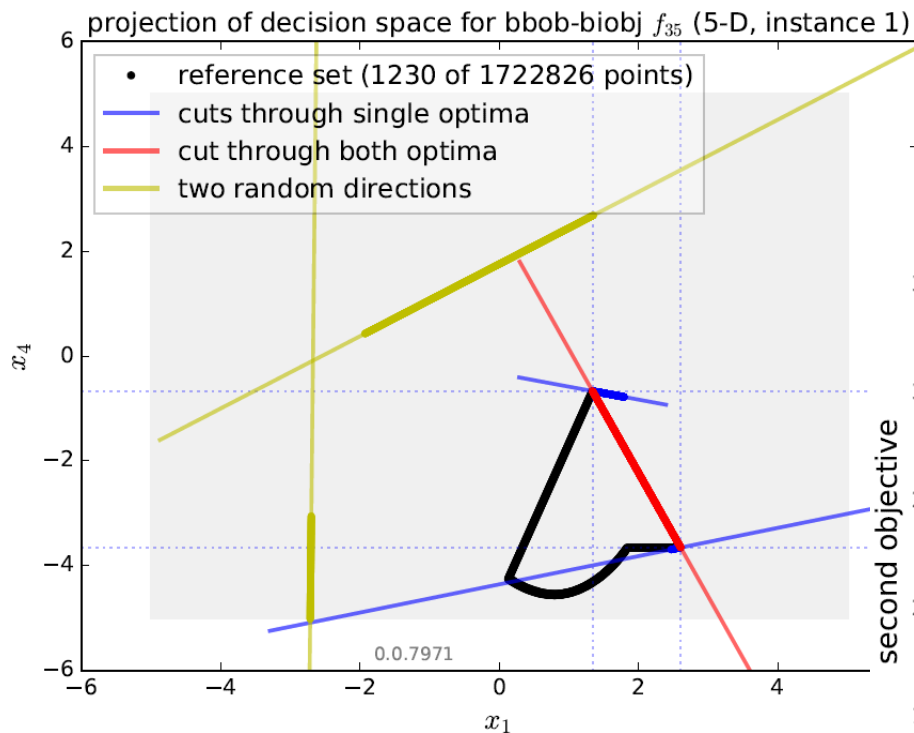
# bbob-biobj Testbed (cont'd)

Example: sphere with sphere



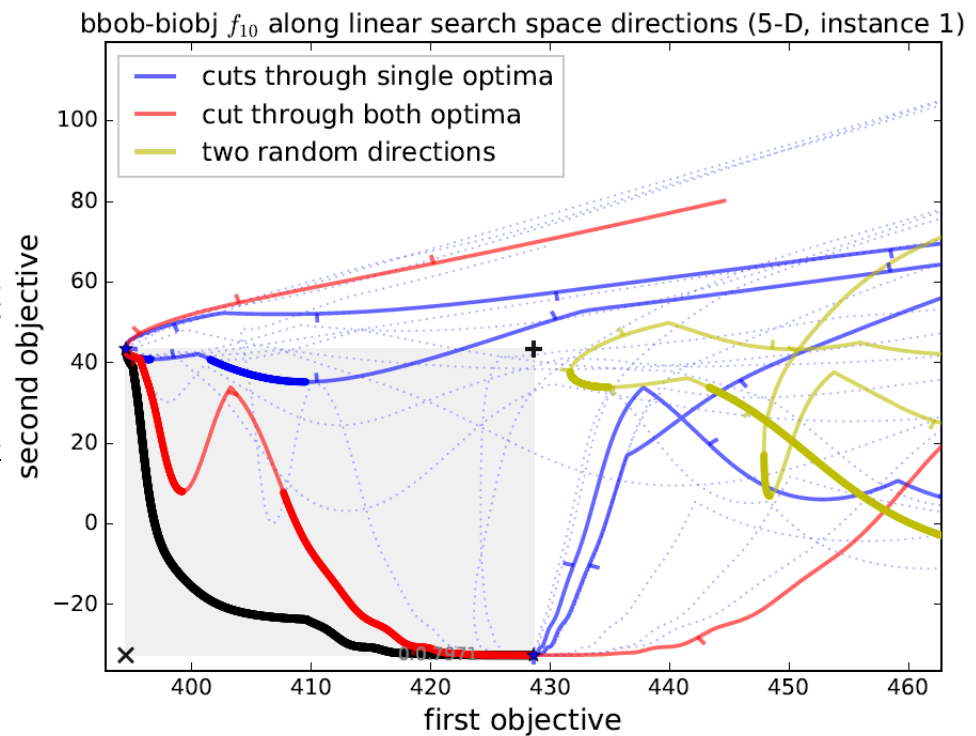
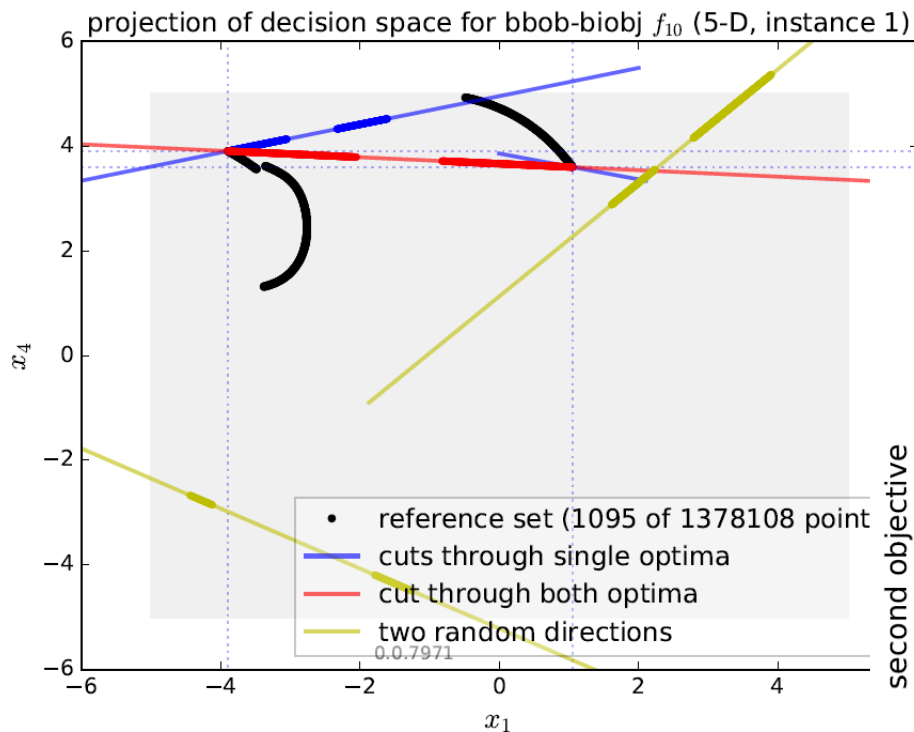
# bbob-biobj Testbed (cont'd)

Example: sharp ridge with sharp ridge



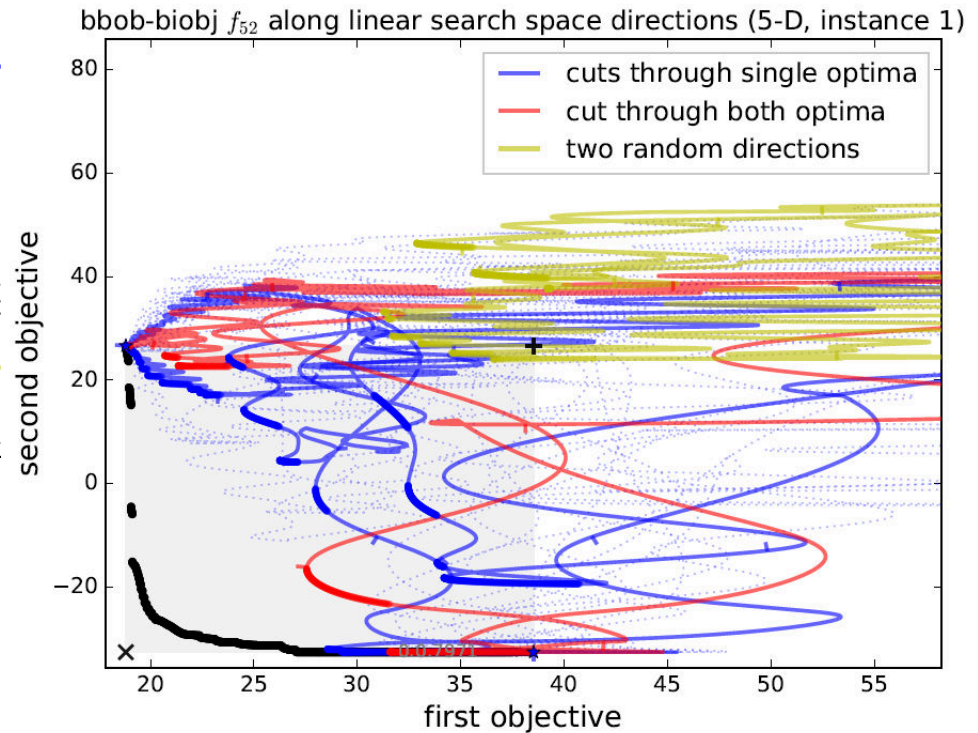
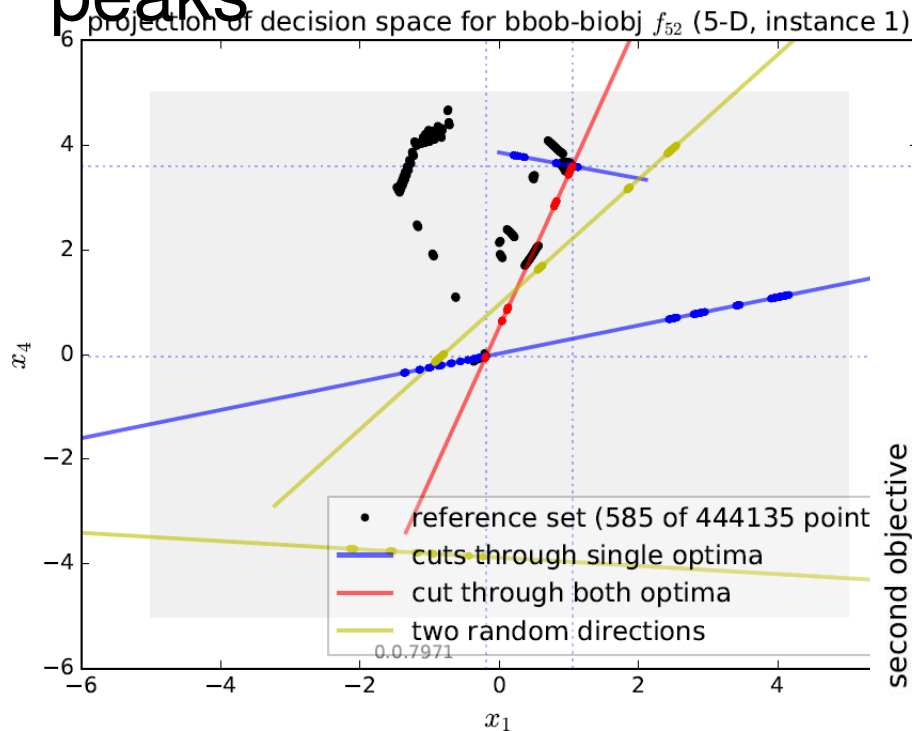
# bbob-biobj Testbed (cont'd)

Example: sphere with Gallagher 101 peaks



# bbob-biobj Testbed (cont'd)

Example: Schaffer F7, cond. 10 with Gallagher 101 peaks



# Exercise

## Objective:

investigate the data you just postprocessed:

- a) which algorithms are the best ones?
- b) does this depend on the dimension?
- c) look at single graphs: can we say something about the algorithms' invariances, e.g. wrt. rotations of the search space?
- d) what's the impact of covariance-matrix-adaptation?
- e) what do you think: are the displayed algorithms well-suited for problems with larger dimension?

**Paper Discussion:**  
**"Dynamic Search in Fireworks Algorithm"**

<http://eprints.cs.univie.ac.at/4082/1/PID3181839.pdf>



## Objectives of the exercise:

- ① Learn how to read an optimization paper critically in order to be able to do high-quality reviews

but also to get the most information from it for practical purposes

- ② Understand the reasoning behind the COCO concepts by looking at how others benchmark optimization algorithms