

Dimensionality reduction and surrogate modelling for high-dimensional UQ problems

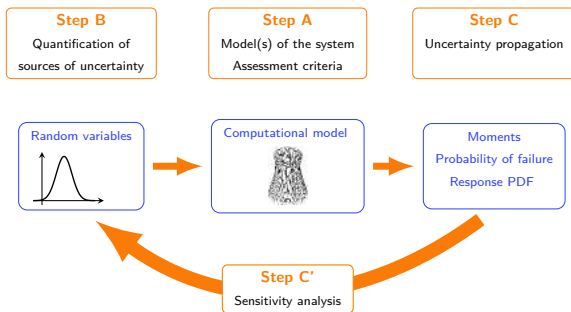
C. Lataniotis, S. Marelli, B. Sudret
Chair of Risk, Safety & Uncertainty Quantification – ETH Zürich



- ① Introduction
- ② Proposed scheme
- ③ Ingredients
- ④ Validation
- ⑤ Summary & Outlook

Problem description

UQ framework



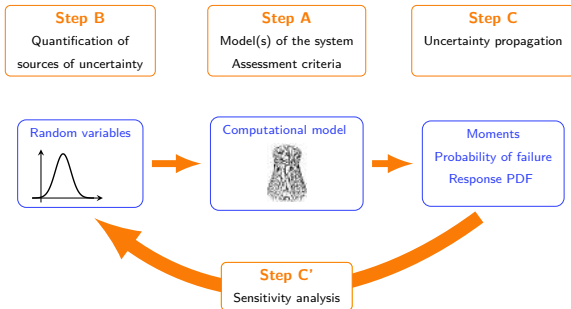
Standard setup

- Prescribed probabilistic model (marginal PDFs and copula)
- Uncertainty propagation by surrogate models (Kriging, PCE)

Sudret, B. (2007). Uncertainty propagation and sensitivity analysis in mechanical models - Contributions to structural reliability and stochastic spectral methods. Habilitation à diriger des recherches, Université Blaise Pascal, Clermont-Ferrand.

Problem description

UQ framework



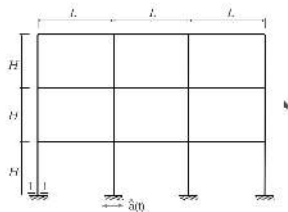
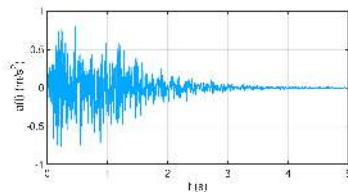
New setup

- High input dimensionality, with possible redundancy in the parameters
- Data sets available instead of prescribed PDFs

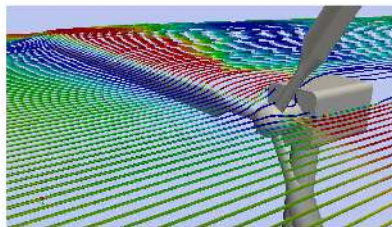
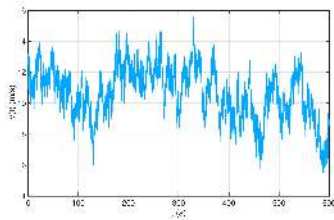
Goal of the PhD: optimally combine dimensionality reduction with surrogate modelling

Applications of Interest

- Earthquake engineering



- Structural health monitoring



Outline

- ① Introduction
- ② Proposed scheme
- ③ Ingredients
- ④ Validation
- ⑤ Summary & Outlook

Key ingredients

Surrogate models (SM)

A surrogate model $\tilde{\mathcal{M}}$ is a function s.t.:

$$\mathcal{M}(\mathbf{x}) = \tilde{\mathcal{M}}(\mathbf{x}; \boldsymbol{\Omega}) + \epsilon$$

- Inexpensive to evaluate
- Depends on configuration parameters $\boldsymbol{\Omega}$
- **Non-intrusive**: parameters are inferred from observations \mathcal{X}, \mathbf{y}

Examples of surrogate models:

- Kriging
- Polynomial chaos expansions
- Low-rank approximations

Dimensionality Reduction (DR)

A transform $\mathcal{X} \in \mathbb{R}^M \mapsto \mathcal{Z} \in \mathbb{R}^m$ of the form

$$\mathbf{z} = g(\mathbf{x}; \mathbf{w})$$

- Preserves some properties of \mathbf{x} (e.g. information content)
- Parameters \mathbf{w} are inferred from observations \mathcal{X}

Examples of DR:

- PCA
- Kernel PCA
- Autoencoders

Methodology

- Given observations

$$\mathcal{X} = \{ \mathbf{x}^{(1)}, \dots, \mathbf{x}^{(N)}; \mathbf{x}^{(i)} \in \mathbb{R}^M \}$$

and system responses

$$\mathbf{y} = \{ y_1 = \mathcal{M}(\mathbf{x}^{(1)}), \dots, y_N = \mathcal{M}(\mathbf{x}^{(N)}) \}$$

- Instead of computing surrogate $\tilde{\mathcal{M}}(\mathbf{x})$
calculate $\tilde{\mathcal{M}}(\mathbf{z})$ where

$$\mathbf{z} = g(\mathbf{x}, \mathbf{w}), \mathbf{z} \in \mathbb{R}^m, m < M$$

- Tune DR parameters \mathbf{w} having the surrogate model performance as objective

Methodology

- Given observations

$$\mathcal{X} = \{ \mathbf{x}^{(1)}, \dots, \mathbf{x}^{(N)}; \mathbf{x}^{(i)} \in \mathbb{R}^M \}$$

and system responses

$$\mathbf{y} = \{ y_1 = \mathcal{M}(\mathbf{x}^{(1)}), \dots, y_N = \mathcal{M}(\mathbf{x}^{(N)}) \}$$

- Instead of computing surrogate $\tilde{\mathcal{M}}(\mathbf{x})$
calculate $\tilde{\mathcal{M}}(\mathbf{z})$ where

$$\mathbf{z} = g(\mathbf{x}, \mathbf{w}), \mathbf{z} \in \mathbb{R}^m, m < M$$

- Tune DR parameters \mathbf{w} having the surrogate model performance as objective

Treats dim. reduction (DR) and surrogate modelling (SM) as **black boxes**

Methodology

- Given observations

$$\mathcal{X} = \{\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(N)}; \mathbf{x}^{(i)} \in \mathbb{R}^M\}$$

and system responses

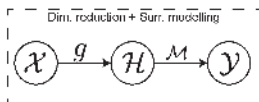
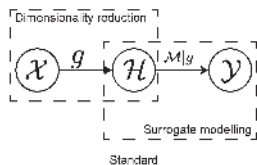
$$\mathbf{y} = \{y_1 = \mathcal{M}(\mathbf{x}^{(1)}), \dots, y_N = \mathcal{M}(\mathbf{x}^{(N)})\}$$

- Instead of computing surrogate $\tilde{\mathcal{M}}(\mathbf{x})$
calculate $\tilde{\mathcal{M}}(\mathbf{z})$ were

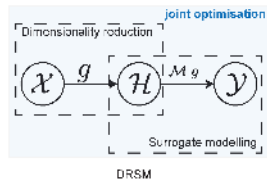
$$\mathbf{z} = g(\mathbf{x}, \mathbf{w}), \mathbf{z} \in \mathbb{R}^m, m < M$$

- Tune DR parameters \mathbf{w} having the surrogate model performance as objective

Treats dim. reduction (DR) and surrogate modelling (SM) as **black boxes**



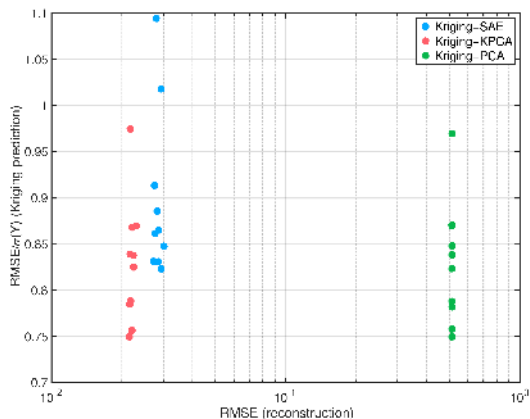
Hinton 2007 (neural network with autoencoder)
Calandra et al. 2016 (GP regression with autoenc.)



Hinton, G. E. and Salakhutdinov, R. S. (2006). Reducing the dimensionality of data with neural networks. *Science* 313, 504–507.

Calandra, R. and Peters J. and Russumen C. E. and Deisenroth M.P. (2016). Manifold Gaussian processes for regression. In *Neural Networks (IJCNN)*, 2016 International Joint Conference, pp. 3338-3345. IEEE.

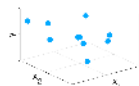
Motivation



Accuracy of surrogate model not correlated with accuracy of dimensionality reduction

DRSM algorithm

Goal: Find optimal \mathbf{w} w.r.t. the surrogate modelling performance of $\tilde{\mathcal{M}}(g(\mathbf{x}, \mathbf{w}))$

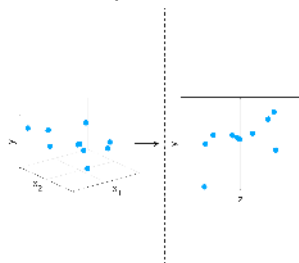


- Given quantities: \mathcal{X}, \mathbf{y}
- Compute \mathbf{w}^* using objective $J(\mathbf{w})$:
 - Compute $\mathcal{Z} = g(\mathcal{X}, \mathbf{w})$
 - Split \mathcal{Z} into training (\mathcal{Z}_t) and test set ($\mathcal{Z}_{\text{test}}$) with $\mathcal{Z}_t \cup \mathcal{Z}_{\text{test}} = \mathcal{Z}$ (resp. \mathbf{y} to $\mathbf{y}_t, \mathbf{y}_{\text{test}}$)
 - Compute surrogate $\tilde{\mathcal{M}}(\mathbf{z})$ using $\mathcal{Z}_t, \mathbf{y}_t$
 - Evaluate the surrogate response $\tilde{\mathcal{M}}(\mathcal{Z}_{\text{test}})$
 - Compute objective (e.g. RMSE):

$$J(\mathbf{w}) = \left(\frac{1}{N_{\text{test}}} \sum_{i=1}^{N_{\text{test}}} \left(y_{\text{test}}^{(i)} - \tilde{\mathcal{M}}(\mathbf{z}_{\text{test}}^{(i)}) \right)^2 \right)^{1/2}$$

DRSM algorithm

Goal: Find optimal \mathbf{w} w.r.t. the surrogate modelling performance of $\tilde{\mathcal{M}}(g(\mathbf{x}, \mathbf{w}))$

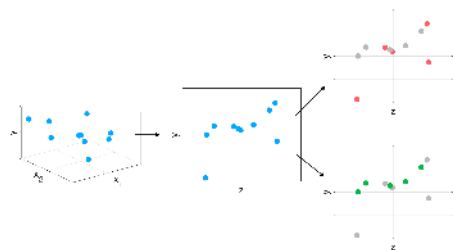


- Given quantities: \mathcal{X}, \mathbf{y}
- Compute \mathbf{w}^* using objective $J(\mathbf{w})$:
 - Compute $\mathcal{Z} = g(\mathcal{X}, \mathbf{w})$
 - Split \mathcal{Z} into training (\mathcal{X}_t) and test set (\mathcal{X}_{cv}) with $\mathcal{Z}_t \cup \mathcal{Z}_{cv} = \mathcal{Z}$ (resp. \mathbf{y} to $\mathbf{y}_t, \mathbf{y}_{cv}$)
 - Compute surrogate $\tilde{\mathcal{M}}(\mathbf{z})$ using $\mathcal{Z}_t, \mathbf{y}_t$
 - Evaluate the surrogate response $\tilde{\mathcal{M}}(\mathcal{Z}_{cv})$
 - Compute objective (e.g. RMSE):

$$J(\mathbf{w}) = \left(\frac{1}{N_{cv} \text{var}(\mathbf{y}_{cv})} \sum_{i=1}^{N_{cv}} \left(\mathbf{y}_{cv}^{(i)} - \tilde{\mathcal{M}}(\mathbf{z}_{cv}^{(i)}) \right)^2 \right)^{1/2}$$

DRSM algorithm

Goal: Find optimal \mathbf{w} w.r.t. the surrogate modelling performance of $\tilde{\mathcal{M}}(g(\mathbf{x}, \mathbf{w}))$

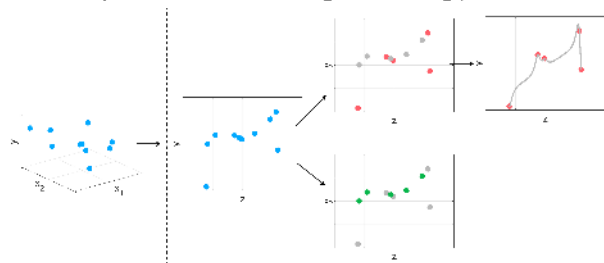


- Given quantities: \mathcal{X}, \mathbf{y}
- Compute \mathbf{w}^* using objective $J(\mathbf{w})$:
 - Compute $\mathcal{Z} = g(\mathcal{X}, \mathbf{w})$
 - Split \mathcal{Z} into training (\mathcal{Z}_t) and test set (\mathcal{Z}_{cv}) with $\mathcal{Z}_t \cup \mathcal{Z}_{cv} = \mathcal{Z}$ (resp. \mathbf{y} to $\mathbf{y}_t, \mathbf{y}_{cv}$)
 - Compute surrogate $\tilde{\mathcal{M}}(\mathbf{z})$ using $\mathcal{Z}_t, \mathbf{y}_t$
 - Evaluate the surrogate response $\tilde{\mathcal{M}}(\mathcal{Z}_{cv})$
 - Compute objective (e.g. RMSE):

$$J(\mathbf{w}) = \left(\frac{1}{N_{cv} \text{var}(\mathbf{y}_{cv})} \sum_{i=1}^{N_{cv}} \left(\mathbf{y}_{cv}^{(i)} - \tilde{\mathcal{M}}(\mathbf{z}_{cv}^{(i)}) \right)^2 \right)^{1/2}$$

DRSM algorithm

Goal: Find optimal \mathbf{w} w.r.t. the surrogate modelling performance of $\tilde{\mathcal{M}}(g(\mathbf{x}, \mathbf{w}))$

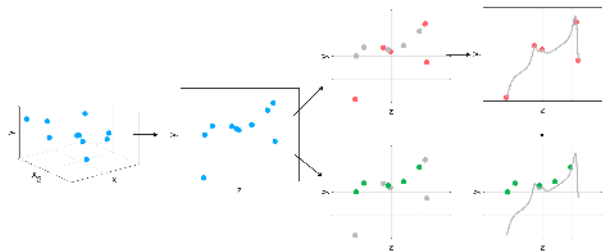


- Given quantities: \mathcal{X}, \mathbf{y}
- Compute \mathbf{w}^* using objective $J(\mathbf{w})$:
 - Compute $\mathcal{Z} = g(\mathcal{X}, \mathbf{w})$
 - Split \mathcal{Z} into training (\mathcal{Z}_t) and test set (\mathcal{Z}_{cv}) with $\mathcal{Z}_t \cup \mathcal{Z}_{cv} = \mathcal{Z}$ (resp. \mathbf{y} to $\mathbf{y}_t, \mathbf{y}_{cv}$)
 - Compute surrogate $\tilde{\mathcal{M}}(\mathbf{z})$ using $\mathcal{Z}_t, \mathbf{y}_t$
 - Evaluate the surrogate response $\tilde{\mathcal{M}}(\mathcal{Z}_{cv})$
 - Compute objective (e.g. RMSE):

$$J(\mathbf{w}) = \left(\frac{1}{N_{cv} \text{var}(\mathbf{y}_{cv})} \sum_{i=1}^{N_{cv}} \left(y_{cv}^{(i)} - \tilde{\mathcal{M}}(\mathbf{z}_{cv}^{(i)}) \right)^2 \right)^{1/2}$$

DRSM algorithm

Goal: Find optimal \mathbf{w} w.r.t. the surrogate modelling performance of $\tilde{\mathcal{M}}(g(\mathbf{x}, \mathbf{w}))$

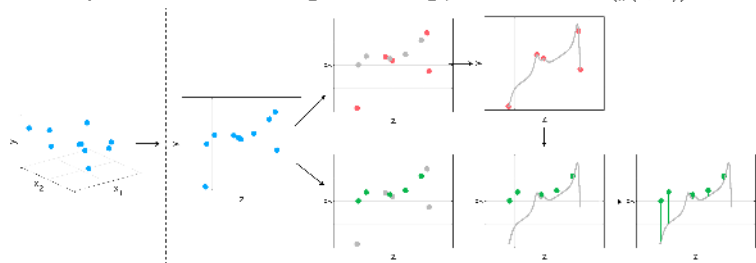


- Given quantities: \mathcal{X}, \mathbf{y}
- Compute \mathbf{w}^* using objective $J(\mathbf{w})$:
 - Compute $\mathcal{Z} = g(\mathcal{X}, \mathbf{w})$
 - Split \mathcal{Z} into training (\mathcal{Z}_t) and test set (\mathcal{Z}_{cv}) with $\mathcal{Z}_t \cup \mathcal{Z}_{cv} = \mathcal{Z}$ (resp. \mathbf{y} to $\mathbf{y}_t, \mathbf{y}_{cv}$)
 - Compute surrogate $\tilde{\mathcal{M}}(\mathbf{z})$ using $\mathcal{Z}_t, \mathbf{y}_t$
 - Evaluate the surrogate response $\tilde{\mathcal{M}}(\mathcal{Z}_{cv})$
 - Compute objective (e.g. RMSE):

$$J(\mathbf{w}) = \left(\frac{1}{N_{cv} \text{var}(\mathbf{y}_{cv})} \sum_{i=1}^{N_{cv}} \left(y_{cv}^{(i)} - \tilde{\mathcal{M}}(\mathbf{z}_{cv}^{(i)}) \right)^2 \right)^{1/2}$$

DRSM algorithm

Goal: Find optimal \mathbf{w} w.r.t. the surrogate modelling performance of $\tilde{\mathcal{M}}(g(\mathbf{x}, \mathbf{w}))$



- Given quantities: \mathcal{X}, \mathbf{y}
- Compute \mathbf{w}^* using objective $J(\mathbf{w})$:
 - Compute $\mathcal{Z} = g(\mathcal{X}, \mathbf{w})$
 - Split \mathcal{Z} into training (\mathcal{Z}_t) and test set (\mathcal{Z}_{cv}) with $\mathcal{Z}_t \cup \mathcal{Z}_{cv} = \mathcal{Z}$ (resp. \mathbf{y} to $\mathbf{y}_t, \mathbf{y}_{cv}$)
 - Compute surrogate $\tilde{\mathcal{M}}(\mathbf{z})$ using $\mathcal{Z}_t, \mathbf{y}_t$
 - Evaluate the surrogate response $\tilde{\mathcal{M}}(\mathcal{Z}_{cv})$
 - Compute objective (e.g. RMSE):

$$J(\mathbf{w}) = \left(\frac{1}{N_{cv} \text{var}(\mathbf{y}_{cv})} \sum_{i=1}^{N_{cv}} \left(\mathbf{y}_{cv}^{(i)} - \tilde{\mathcal{M}}(\mathbf{z}_{cv}^{(i)}) \right)^2 \right)^{1/2}$$

Summary

DRSM ingredients

- Dimensionality reduction method
- Surrogate modelling method
- Objective function type
- Optimisation method

Remarks

- Only the forward DR step is required
- Simplified SMs favour computational efficiency
- Multiple CV-folds are preferred. Extreme case: *Leave-One-Out error*
- Global optimisation is expected to perform better

Summary

DRSM ingredients

- Dimensionality reduction method : Kernel PCA
- Surrogate modelling method : Kriging
- Objective function type : Leave-One-Out RMSE
- Optimisation method : Genetic algorithm with BFGS refinement

Remarks

- Only the forward DR step is required
- Simplified SMs favour computational efficiency
- Multiple CV-folds are preferred. Extreme case: *Leave-One-Out error*
- Global optimisation is expected to perform better

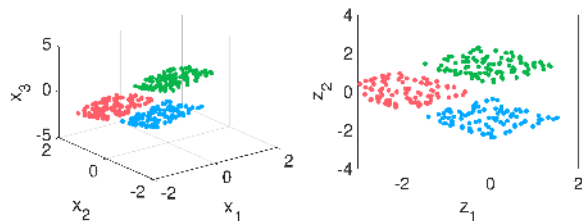
One particular DRSM setup is explored next

Outline

- ① Introduction
- ② Proposed scheme
- ③ Ingredients**
- ④ Validation
- ⑤ Summary & Outlook

Kernel PCA

Recall PCA:



- Calculate the covariance matrix $C = \text{cov}(\mathcal{X})$
- Compute the eigen-decomposition of C :

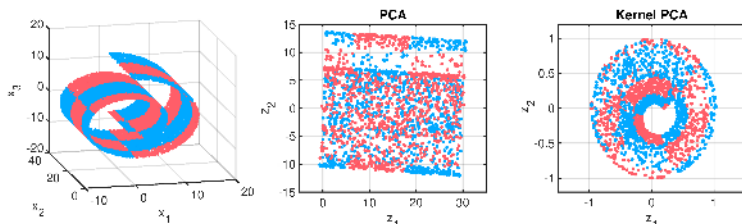
$$Cv = \lambda v$$

- Keep V , an $M \times m$ collection of m eigenvectors v with largest eigenvalues λ
- Obtain \mathcal{Z} by projecting \mathcal{X} onto V :

$$\mathcal{Z} = \mathcal{X}V$$

Kernel PCA

Kernel PCA (KPCA) is a non-linear extension of PCA



- First maps the input to a high dimensional space (*feature space*):

$$\mathbf{x} \in \mathcal{R}^M \rightarrow \Phi(\mathbf{x}) \in \mathcal{H}$$

then PCA is performed in this space

- Infinite dimensional** feature spaces are a common choice
- Calculates \mathcal{Z} as projections onto the first m eigenvectors of $C_{\mathcal{H}} = \text{cov}[\Phi(\mathcal{X})]$

Problem: In general, $C_{\mathcal{H}}$ and its eigenvectors **cannot** be computed

Kernel PCA

How to solve the eigen-decomposition problem in \mathcal{H}

- Consider Φ that:

$$\kappa(\mathbf{x}_i, \mathbf{x}_j) = \Phi(\mathbf{x}_i) \cdot \Phi(\mathbf{x}_j)$$

- Although $v_i \rightarrow$ infinite dimensional, $N \rightarrow$ finite, thus:

$$\mathbf{v}_i = \sum_{j=1}^N \alpha_j^{(i)} \Phi(\mathbf{x}_j), \quad i = 1, \dots, m$$

where $\alpha^{(i)}$: the **expansion coefficients** of v_i

- The eigen-decomposition problem:

$$\lambda \mathbf{v} = \mathbf{C}_{\mathcal{H}} \mathbf{v}$$

can be cast as:

$$\lambda \boldsymbol{\alpha} = \frac{1}{N} \mathbf{K} \boldsymbol{\alpha}$$

where \mathbf{K} is the $N \times N$ kernel matrix with elements $K_{ij} = \kappa(\mathbf{x}_i, \mathbf{x}_j)$

By solving this eigen-decomposition the coefficients $\boldsymbol{\alpha}$ are obtained (not v !)

Kernel PCA

How to calculate \mathcal{Z}

The k -th component of the i -th sample of \mathcal{Z} , denoted by $z_i^{(k)}$, is the projection of $\Phi(\mathbf{x}_i)$ onto \mathbf{v}_k :

$$\begin{aligned} z_i^{(k)} &= \Phi(\mathbf{x}_i)^T \mathbf{v}_k \\ &= \sum_{j=1}^N \alpha_j^{(k)} \Phi(\mathbf{x}_i)^T \Phi(\mathbf{x}_j) \\ &= \sum_{j=1}^N \alpha_j^{(k)} \kappa(\mathbf{x}_i, \mathbf{x}_j) \end{aligned}$$

Remarks

- Some details are omitted here (e.g. centering the kernel)
- In contrast to PCA going from \mathcal{Z} back to \mathcal{X} is non-trivial (**pre-image problem**)
- The **ARD** kernel will be used:

$$\kappa(\mathbf{x}_i, \mathbf{x}_j; \mathbf{w}) = \exp \left(-\frac{1}{2} \sum_{k=1}^M \frac{1}{w_k^2} (x_i^{(k)} - x_j^{(k)})^2 \right)$$

Schölkopf, B., Smola, A. J., and Müller, K.-R., (1999). Kernel Principal Component Analysis, *Advances in Kernel Methods-Support Vector Learning*, MIT Press, Cambridge, MA pp. 327-352.

Ham, J., Lee, D. D., Mika, S., and Schölkopf, B. (2004). A kernel view of the dimensionality reduction of manifolds. In *Proceedings of the twenty-first international conference on Machine learning* (p. 47), ACM.

Kriging reminder

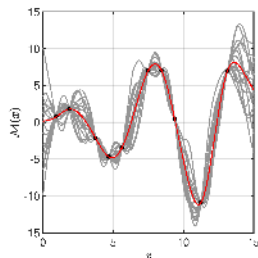
Kriging metamodeling in a nutshell

Universal Kriging:

$$\tilde{\mathcal{M}}(\mathbf{x}) = \beta^T \mathbf{f}(\mathbf{x}) + \sigma^2 Z(\mathbf{x}, R(\mathbf{x}, \mathbf{x}_{ED}; \hat{\theta}))$$

$$\hat{\theta} = \arg \min J(\hat{\theta})$$

Objective function varies depending on the estimation method (e.g. **maximum likelihood**, **cross-validation**, etc.)



Using a Kriging metamodel as a surrogate

A Kriging metamodel forms a group of curves characterized by their:

- Mean (model output):

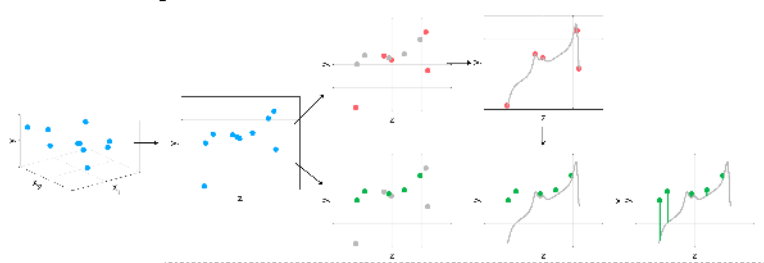
$$\mu_{\hat{Y}}(\mathbf{x}) = \mathbf{f}(\mathbf{x})^T \boldsymbol{\beta} + \mathbf{r}(\mathbf{x})^T \mathbf{R}^{-1} (\mathbf{y} - \mathbf{F}\boldsymbol{\beta})$$

- Variance (local error estimate):

$$\sigma_{\hat{Y}}^2(\mathbf{x}) = \sigma^2 \left(1 - \mathbf{r}^T(\mathbf{x}) \mathbf{R}^{-1} \mathbf{r}(\mathbf{x}) + \mathbf{u}^T(\mathbf{x}) (\mathbf{F}^T \mathbf{R}^{-1} \mathbf{F})^{-1} \mathbf{u}(\mathbf{x}) \right)$$

DRSM objective: Kriging Leave-One-Out error

Recall DRSM algorithm

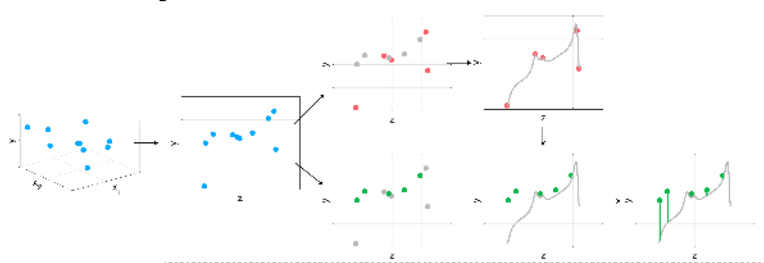


The Leave-One-Out RMSE error reads:

$$J(\mathbf{w}) = \left(\frac{1}{N \text{Var}[\mathbf{y}]} \sum_{i=1}^N (\mathcal{M}(z_i) - \mu_{\hat{\mathbf{y}}, (-i)}(z_i))^2 \right)^{1/2}$$

DRSM objective: Kriging Leave-One-Out error

Recall DRSM algorithm



The Leave-One-Out RMSE error reads:

$$J(\mathbf{w}) = \left(\frac{1}{N \text{Var}[\mathbf{y}]} \sum_{i=1}^N (\mathcal{M}(\mathbf{z}_i) - \mu_{\hat{\mathcal{Y}}_{i,(-i)}}(\mathbf{z}_i))^2 \right)^{1/2}$$

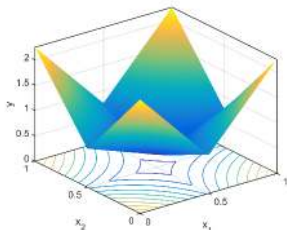
For Kriging surrogates $\mu_{\hat{\mathcal{Y}}_{i,(-i)}}(\mathbf{z}_i)$ can be computed efficiently

Outline

- ① Introduction
- ② Proposed scheme
- ③ Ingredients
- ④ Validation**
- ⑤ Summary & Outlook

Sobol function

Model description



$$\mathcal{M}(\mathbf{x}) = \prod_{i=1}^{20} \frac{|4x_i - 2| + \alpha_i}{1 + a_i}, \quad x_i \in [0, 1]$$

where

$$\boldsymbol{\alpha} = [1, 2, 5, 10, 20, 50, 100, 500, , \dots, 500]^T$$

DRSM parameters

KPCA

Kernel: ARD

Kriging

Correlation function: Matérn 5/2 (isotropic)

Trend type: linear

Optimisation: GA + BFGS

Optimisation

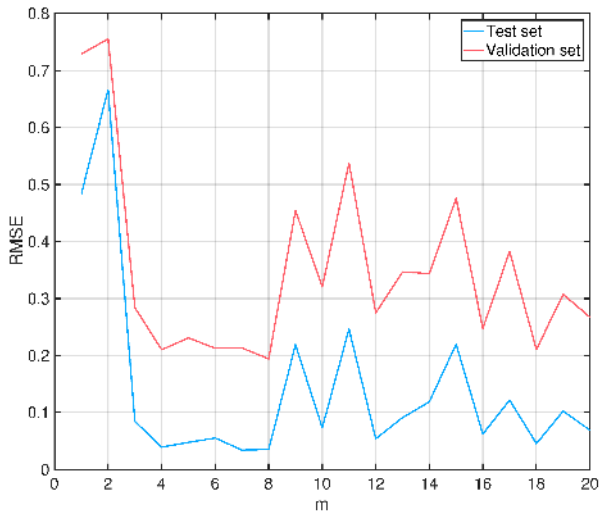
Method: GA+ BFGS

Population size: 60

Max. Iterations: 100

Conv. tolerance: 10^{-3}

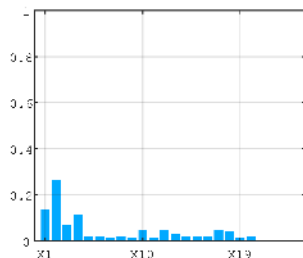
Training: 400 random samples
Validation: 1000 random samples

Sobol function: m vs surrogate model performanceSelected $m = 1$

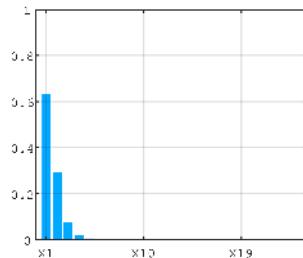
Sobol function: Optimal KPCA parameters ($m = 4$)

ARD Kernel reminder:

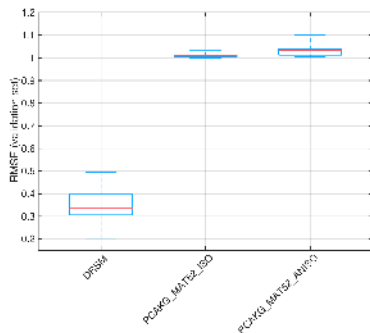
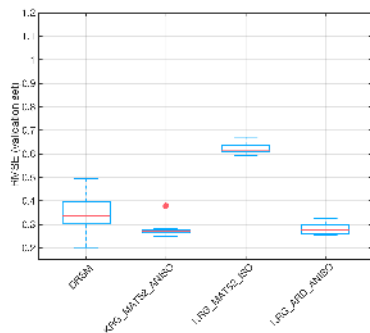
$$\kappa(\mathbf{x}_i, \mathbf{x}_j; \mathbf{w}) = \exp \left(-\frac{1}{2} \sum_{k=1}^M \frac{1}{w_k^2} (x_i^{(k)} - x_j^{(k)})^2 \right)$$

 $1/w_k$ (ARD kernel)

Global sensitivity analysis

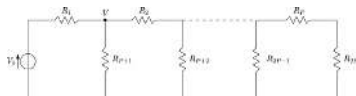


DRSM vs plain Kriging



Electrical resistor networks

Dataset description



- Courtesy of **SANDIA National Labs**
- Network comprised of 80 uncertain resistors
- Output of interest is voltage at V
- Effect of resistors to V decays with distance

DRSM parameters

KPCA

Kernel: ARD

Kriging

Correlation function: Matérn 5/2 (isotropic)

Trend type: linear

Optimisation: GA + BFGS

Optimisation

Method: GA + BFGS

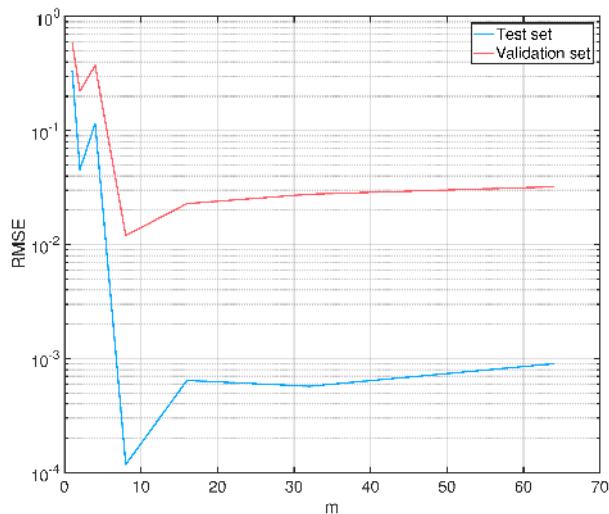
Population size: 150

Max. Iterations: 100

Conv. tolerance: 10^{-3}

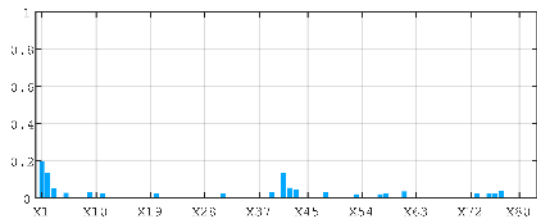
Training: 500 samples
Validation: 500 samples

Jakeman, D., Michael S. E., and Khachik S. (2015). Enhancing l1-minimization estimates of polynomial chaos expansions using basis selection. *Journal of Computational Physics* 289, pp. 18-34.

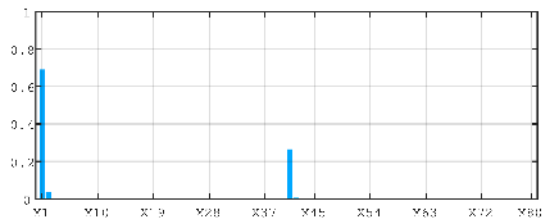
Resistor networks: m vs surrogate model performanceSelected $m = 8$

Resistor networks: Optimal KPCA parameters ($m = 8$)

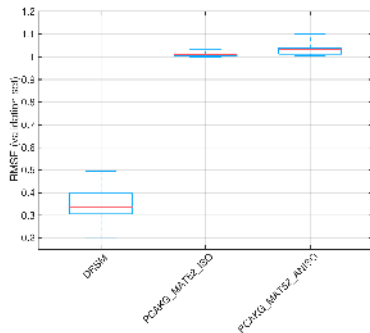
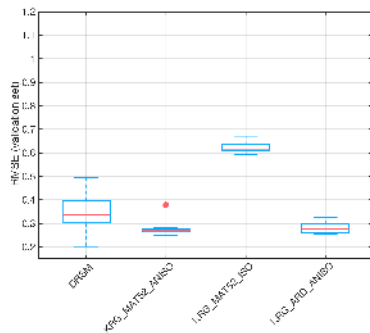
$1/w_i$
(ARD kernel)



Global sensitivity
analysis



Resistor networks: DRSM vs plain Kriging



Outline

- ① Introduction
- ② Proposed scheme
- ③ Ingredients
- ④ Validation
- ⑤ Summary & Outlook

Summary & Outlook

Summary

- A new framework for SM with high-dimensional inputs is proposed
- It is currently at validation stage
- It shows superior performance compared to traditional approaches (disjoint DR and SM)
- An interesting by-product of DRSM with KPCA using ARD kernel: pseudo-sensitivity indices

Outlook

- Explore different setups, e.g. PCE instead of Kriging and Autoencoders instead of KPCA
- Test performance of various DRSM set-ups on problems of interest (e.g. time-series inputs)

Summary & Outlook

Summary

- A new framework for SM with high-dimensional inputs is proposed
- It is currently at validation stage
- It shows superior performance compared to traditional approaches (disjoint DR and SM)
- An interesting by-product of DRSM with KPCA using ARD kernel: pseudo-sensitivity indices

Outlook

- Explore different setups, e.g. PCE instead of Kriging and Autoencoders instead of KPCA
- Test performance of various DRSM set-ups on problems of interest (e.g. time-series inputs)

Thank you very much for your attention!



UQLAB

The Framework for Uncertainty Quantification

www.uqlab.com

Chair of Risk, Safety & Uncertainty Quantification

<http://www.rsuq.ethz.ch>